

Sample Size Calculation

National Cancer Center, Japan

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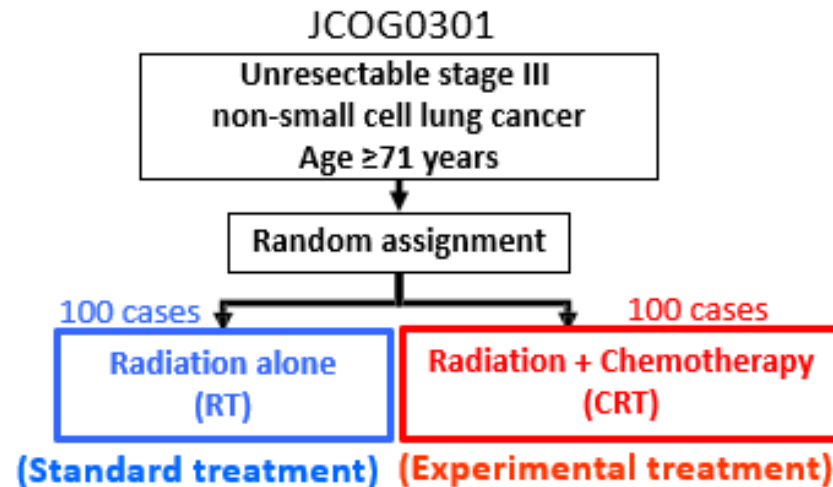
Junki Mizusawa

Objective of this lecture

- As a clinician, learn what you need to know about sample size calculations
 - What to consider when consulting a statistician?
 - What information is needed for the sample size calculation?
 - What do statisticians think?
- Understand sample size calculations to better understand study design
 - Superiority and noninferiority tests
 - Risk-benefit balance

Directions for Sample Size Calculation

Example of Sample Size Description in an Article: Superiority Test



Statistical analysis

The trial was designed to have 80% power to detect a 5-month difference in median overall survival (15 months in the chemoradiotherapy group and 10 months in the radiotherapy alone group) via a log-rank test with one-sided alpha of 0.05.^{7,10-12} A sample size of 200 patients was planned by the Schoenfeld and Richter method,¹³ with 1.5 years of follow-up after 4 years of patient accrual.

Thoracic radiotherapy with or without daily low-dose carboplatin in elderly patients with non-small-cell lung cancer: a randomised, controlled, phase 3 trial by the Japan Clinical Oncology Group (JCOG0301)

Shinji Atagi, Masao Kawaihara, Akira Yokoyama, Hiroaki Okamoto, Nobuyuki Yamamoto, Yutshiro Ohe, Toshiyuki Sawa, Satoshi Ishikawa, Taro Shibata, Haruhiko Fukuda, Nagahiro Suga, Tomohide Tamura, on behalf of the Japan Clinical Oncology Group Lung Cancer Study Group

Summary

Background It is unknown whether combined chemoradiotherapy improves overall survival in elderly patients with locally advanced non-small-cell lung cancer (NSCLC). The aim of this study was to assess whether radiotherapy plus carboplatin results in longer survival than radiotherapy alone in elderly patients with NSCLC.

Methods This was a randomised, controlled, phase 3 trial by the Japan Clinical Oncology Group (JCOG0301). Patients older than 70 years with unresectable stage III NSCLC were randomly assigned to chemoradiotherapy (50 Gy plus concurrent low-dose carboplatin [10 mg/m² per day, 5 days a week for 30 days] or radiotherapy alone, using a minimisation method with biased-coins assignment balancing on Eastern Cooperative Oncology Group (ECOG) performance status (0 vs 1 vs 2), stage (IIIA vs IIIB), and institution. The primary endpoint was overall survival, which was analysed for the eligible population and stratified by ECOG performance status, stage, and institution. The trial was stopped early as a result of the second planned interim analysis. This study is registered with UMIN Clinical Trials Registry, number C000000060, and ClinicalTrials.gov, number NCT00132665.

Findings 200 patients were enrolled from Sept 1, 2003 to May 27, 2010: 100 in the chemoradiotherapy group and 100 in the radiotherapy group. The second planned interim analysis was done 10 months after completion of patient accrual. At this time, median follow-up for censored cases was 16.4 months (95% CI 14.3-17.5). In accordance with the

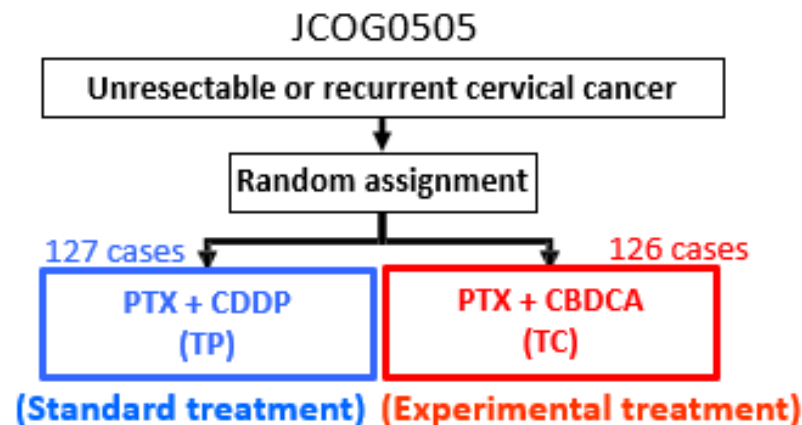
publication of this all survival for the and 16-9 months (p value=0.0179). In the radiotherapy fromocytopenia (12-35%) than ility were similar temocradiotherapy

temocradiotherapy opulation.

group—the Japan [JCOG0301]—was r-dose carboplatin on survival than with unresectable was stopped early red in four of ene in the chemo- ly assessed radio- 8 of 45 evaluable hat were protocol- or normal lung treatment-related

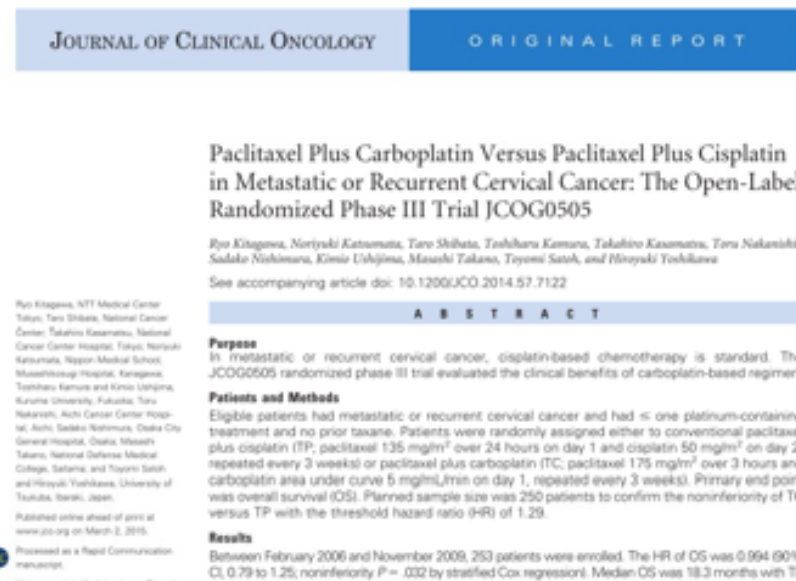
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Example of Sample Size Description in an Article: Noninferiority Test



Statistical Design and Analysis

Initially, with an accrual time of 2.5 years and minimum follow-up period of 1 year, the required number of OS events was 209 and the planned sample size was 250 according to the Schoenfeld and Richter method¹⁷ to confirm the noninferiority of TC compared with TP, with a one-sided α level of 0.05 and power of at least 70%, with noninferiority margin of 1.29, corresponding to 2 months in OS, assuming a median OS in the TP group of 9 months based on outcome in the GOG 169 trial (SCC only).



† metastatic or recurrent cervical cancer patients who received platinum agents.

be administered over 24 hours to reduce toxicity when combined with cisplatin; an inpatient hospital stay for

has been reported to be a less toxic analog than cisplatin for cervical cancer. These agents have not been compared in phase III trials. Carboplatin induces less toxicity, less nausea/vomiting, and less myelosuppression than cisplatin.¹⁰ The combination of paclitaxel and carboplatin allows for administration over 3 hours, and carboplatin requires no hydration. In the first multicenter phase II trial of paclitaxel and carboplatin in metastatic or advanced cervical

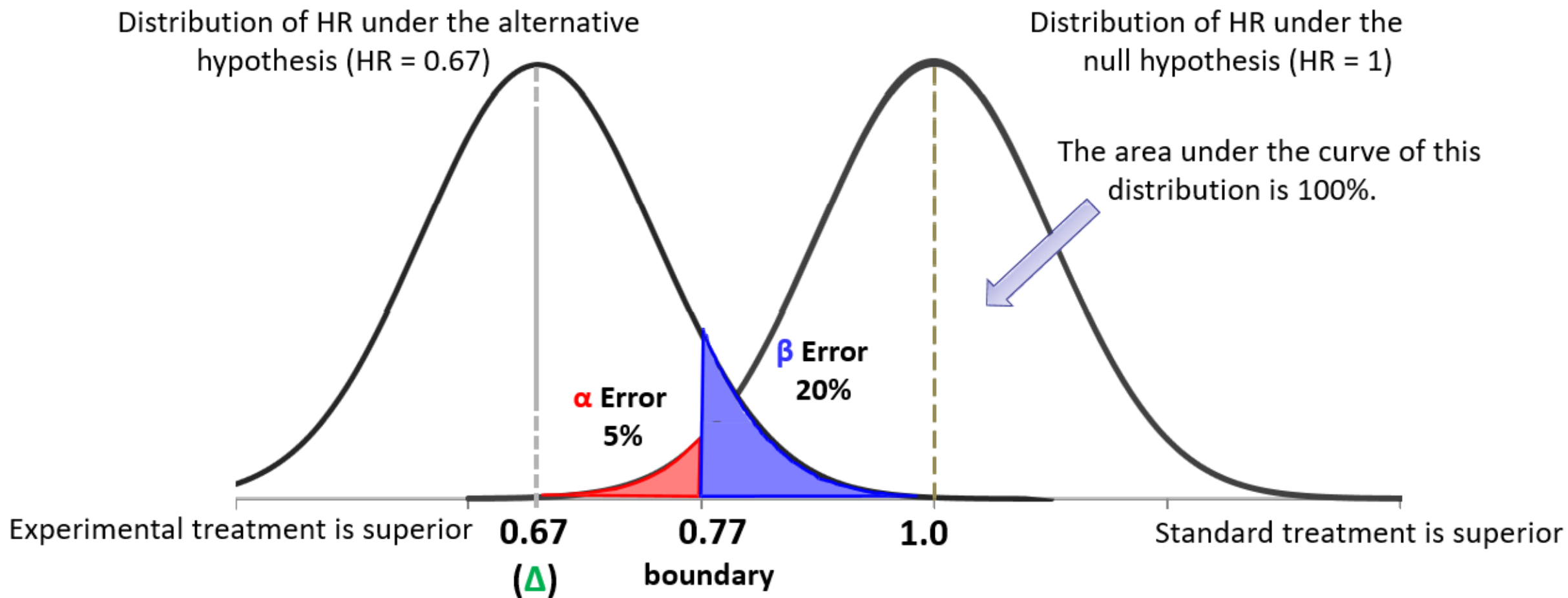
Kitagawa et al. (2015) J Clin Oncol.

Basic Principles of Sample Size Calculation

The required sample size determined in sample size calculations is established to satisfy the following conditions:

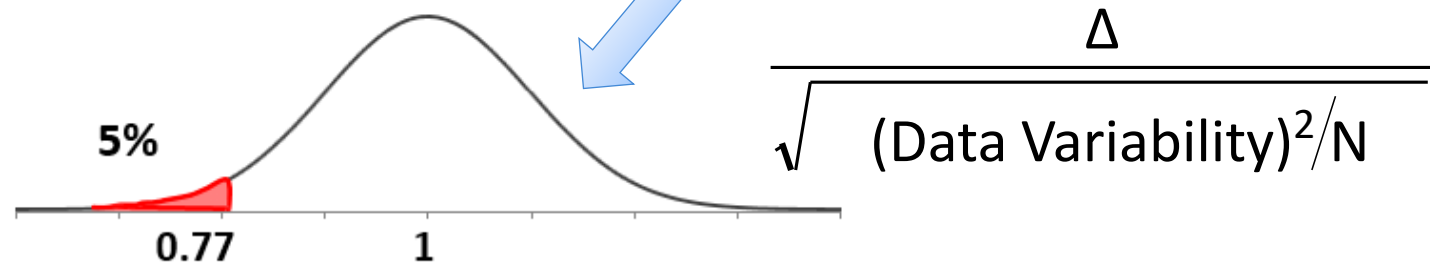
1. Suppress the probability (α) of mistakenly judging that a new treatment is effective when the null hypothesis is correct below a specified threshold
2. Maintain the probability of correctly judging that a new treatment is effective (**power** $[1 - \beta]$) when the true effect of the new treatment is Δ (when the alternative hypothesis is correct)

Distribution of HR Obtained as α , β , and Δ

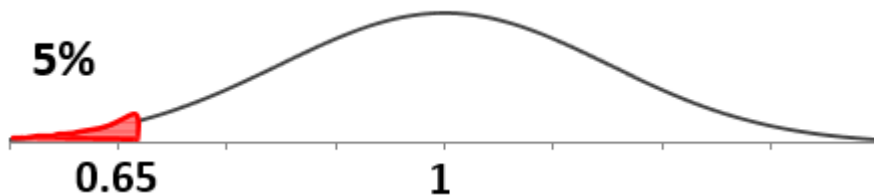


Relationship between Sample Size and Distribution of the Test Statistic

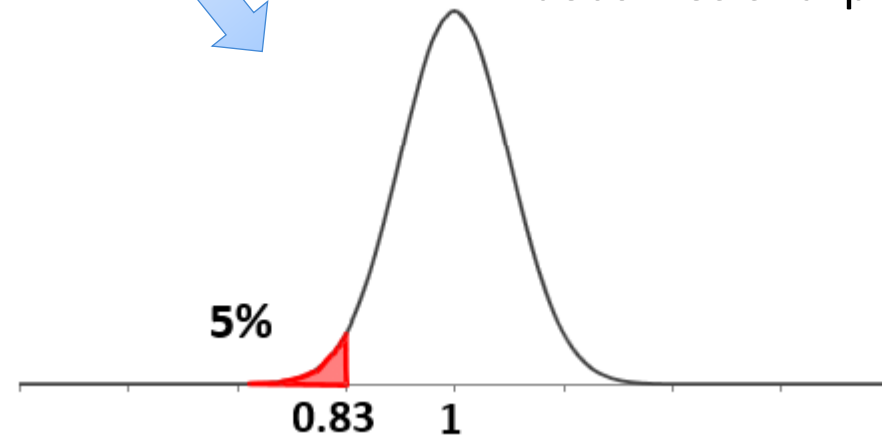
N is included in the formula defining the distribution of the test statistic



As N decreases, the distribution becomes more gradual.



As N increases, the distribution becomes sharp.



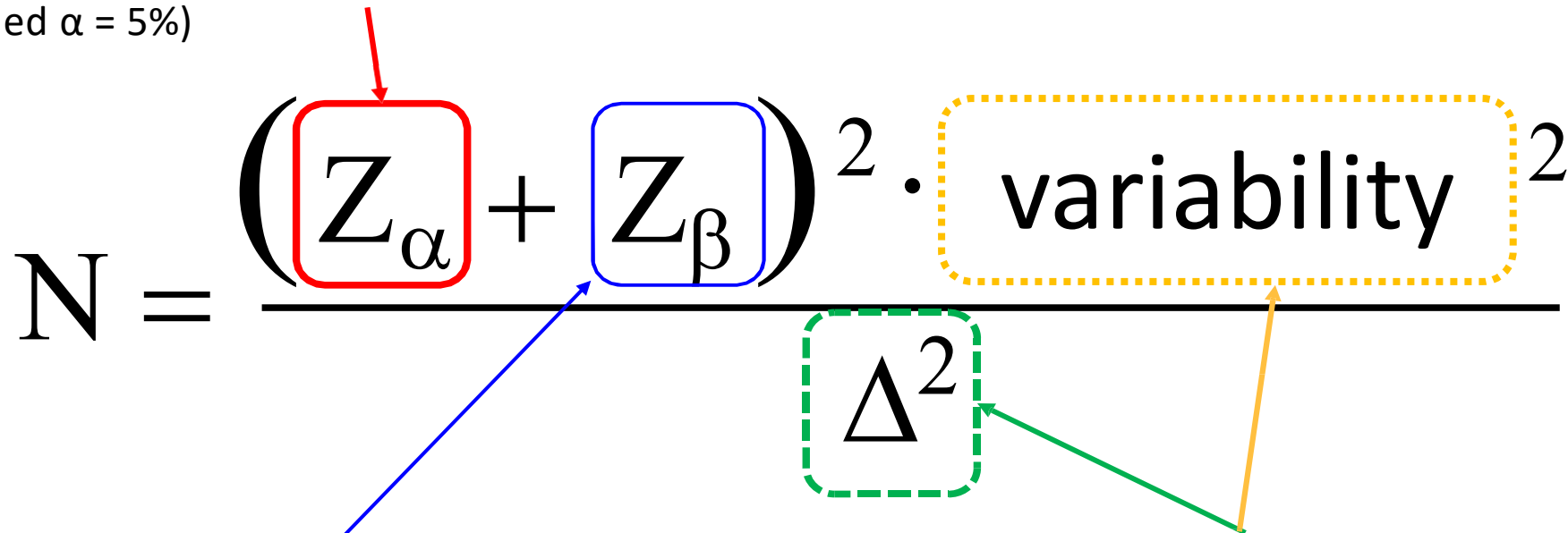
$$\frac{\Delta}{\sqrt{(\text{Data Variability})^2/N}}$$

Framework for Sample Size Calculation

Define **N** so that the distribution
of the test statistic satisfies

α , β , and Δ

Substitute the value corresponding to the significance level α
(1.96 if one-sided $\alpha = 2.5\%$ and two-sided $\alpha = 5\%$ and
1.64 if one-sided $\alpha = 5\%$)

$$N = \frac{\left(Z_{\alpha} + Z_{\beta} \right)^2 \cdot \text{variability}^2}{\Delta^2}$$


The format in which the data is entered depends on the outcome type
(continuous variable, binary data, time-to event) and test method

Enter the value corresponding to power
(0.84 if power = 80% and 1.28 if power = 90%)

Framework of the Sample Size Formula for Each Test Method

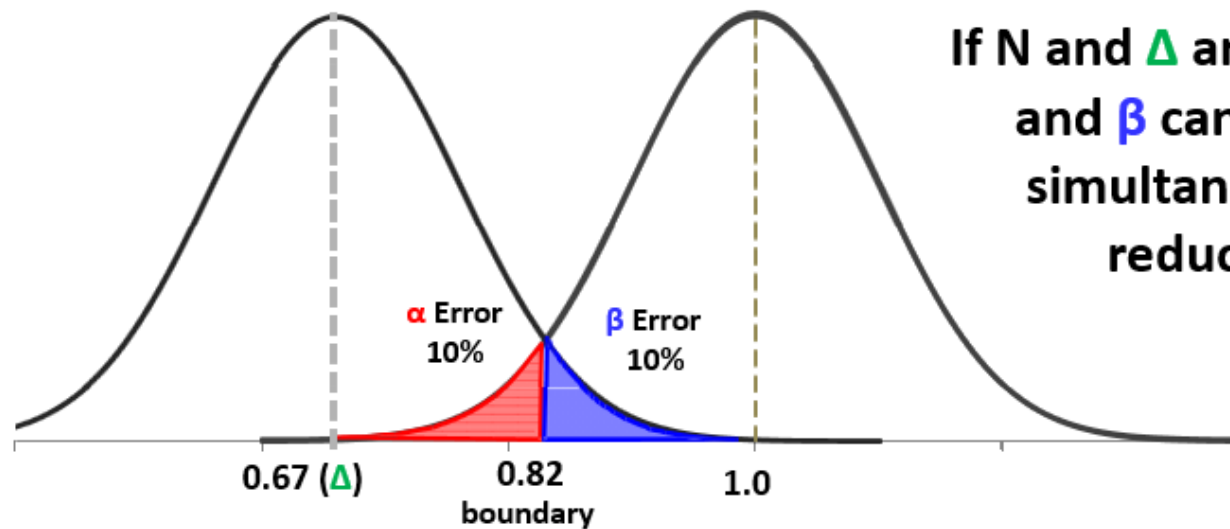
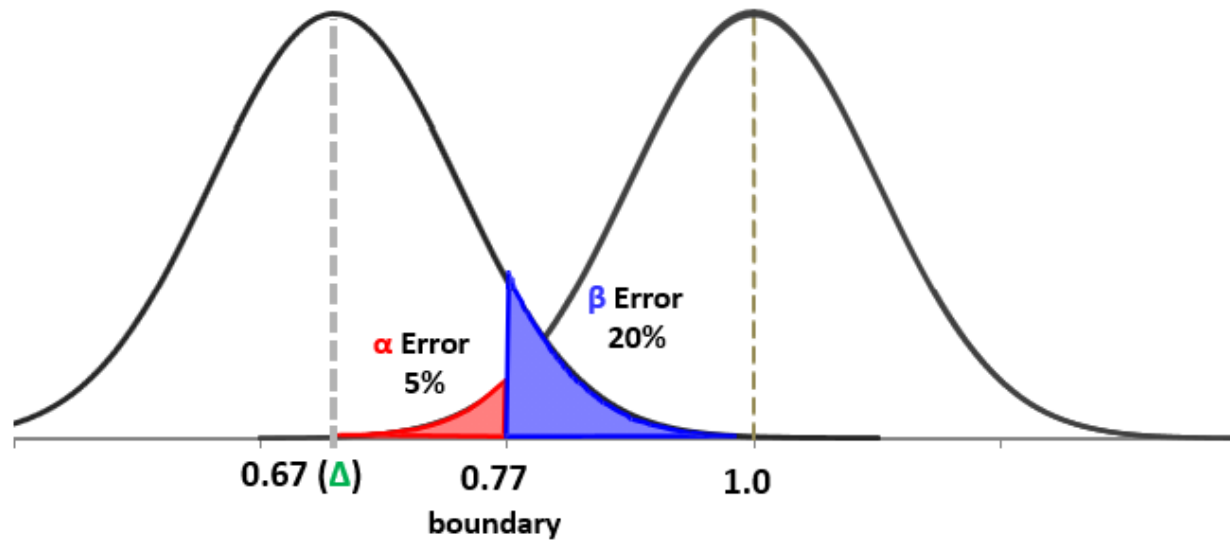
$$t\text{-test: } N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot (\text{Data Variability})^2}{(\text{Difference of mean})^2}$$

$$\chi^2 \text{ Test: } N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot \left[\begin{array}{l} \text{Proportion of standard group (1 - Proportion of standard group)} \\ + \text{Proportion of study group (1 - Proportion of study groups)} \end{array} \right]^2}{(\text{Proportion difference})^2}$$

$$\text{log rank test: } N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot \left[\begin{array}{l} \text{The value considering the prognosis} \\ \text{and enrollment/follow-up period.} \end{array} \right]}{\ln(\text{HR})^2}$$

α and β are Trade-offs

$$N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot \text{Variability}^2}{\Delta^2}$$

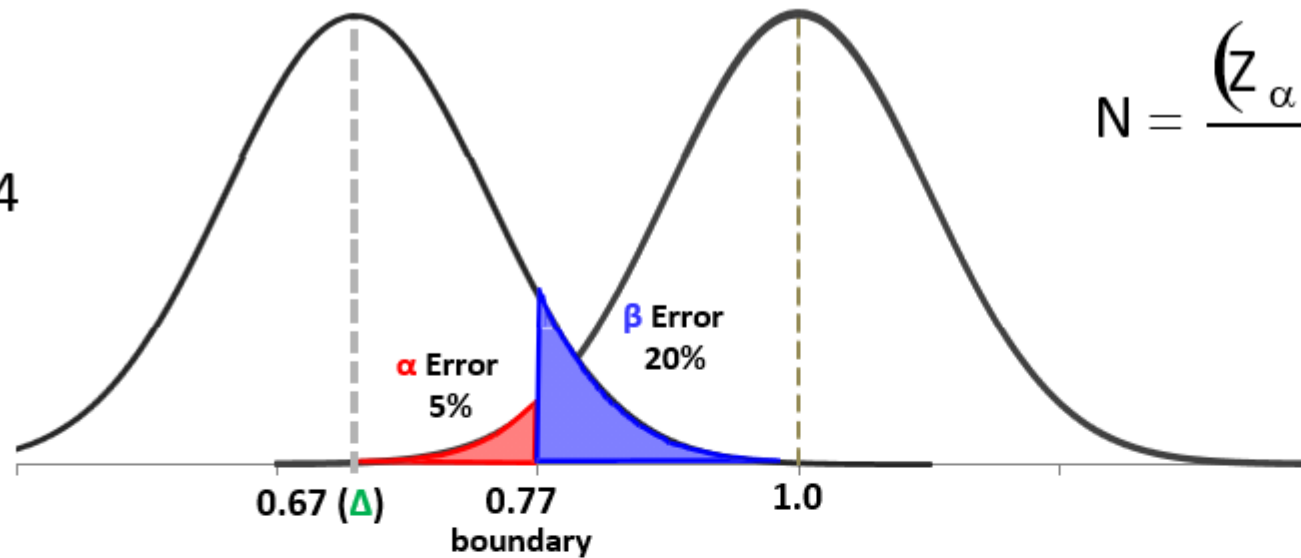


If N and Δ are fixed, α and β cannot be simultaneously reduced

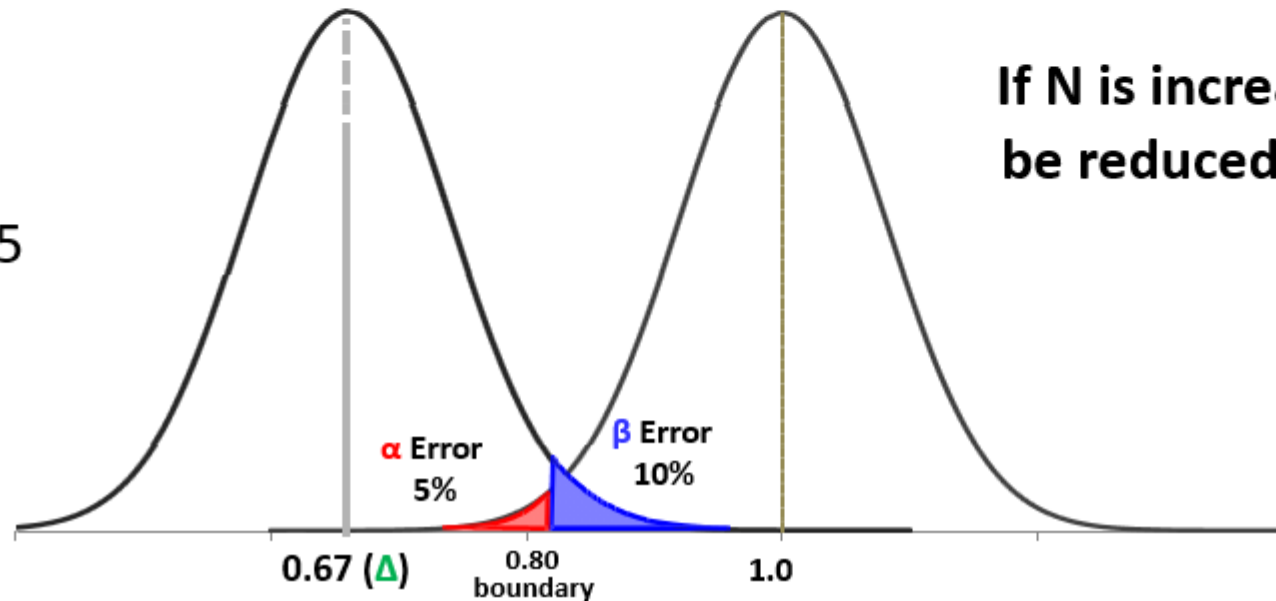
If You Increase N, Power can be Increased by Fixing α

$$N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot \text{Variability}^2}{\Delta^2}$$

N = 174



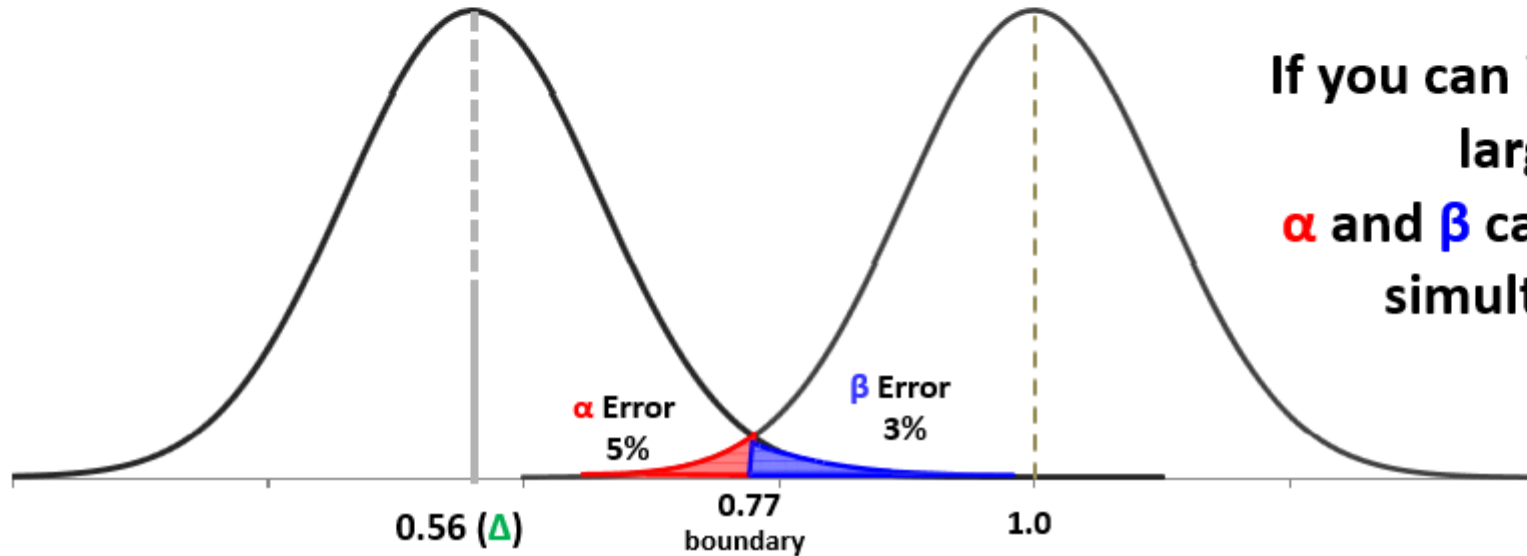
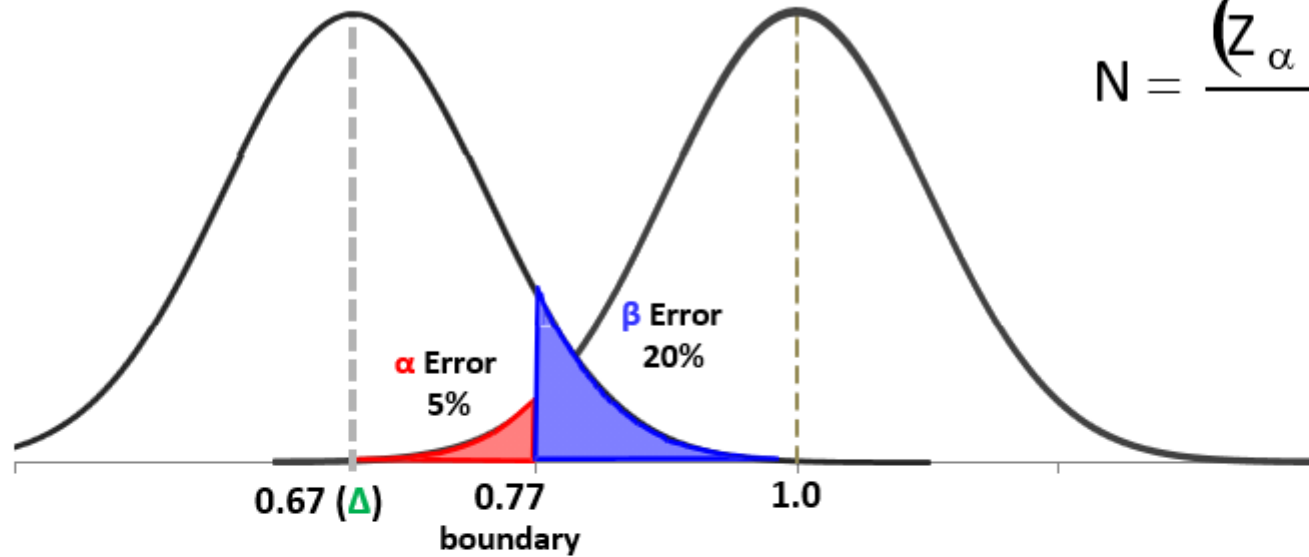
N = 245



If N is increased, α and β can be reduced simultaneously

If You Can Increase Δ , You Can Fix α and Increase Power

$$N = \frac{(Z_{\alpha} + Z_{\beta})^2 \cdot \text{Variability}^2}{\Delta^2}$$



If you can increase Δ to a large size,
 α and β can be reduced simultaneously

Memorize!

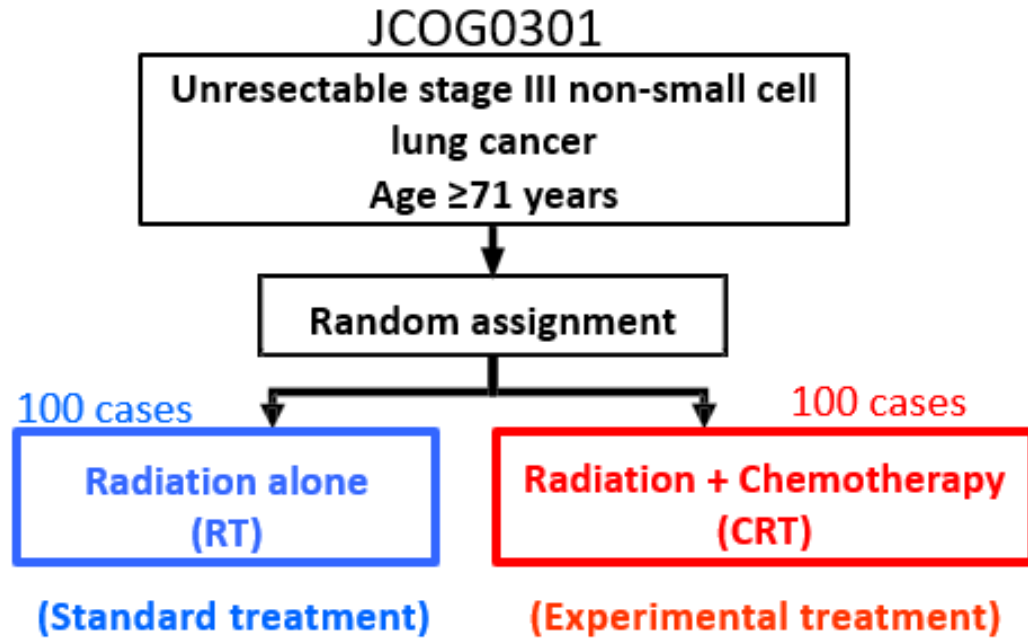
Minimum Parameters Required for Sample Size Calculation

- Size of treatment effect: Δ (delta)
- Variability
- Significance level: α (alpha)
 - The value below which the P value is considered to indicate a “significant difference”
- Power: $1-\beta$ (1-beta, power)
 - The probability of correctly determining that a truly effective treatment is effective

Things to Consider When Setting Parameters

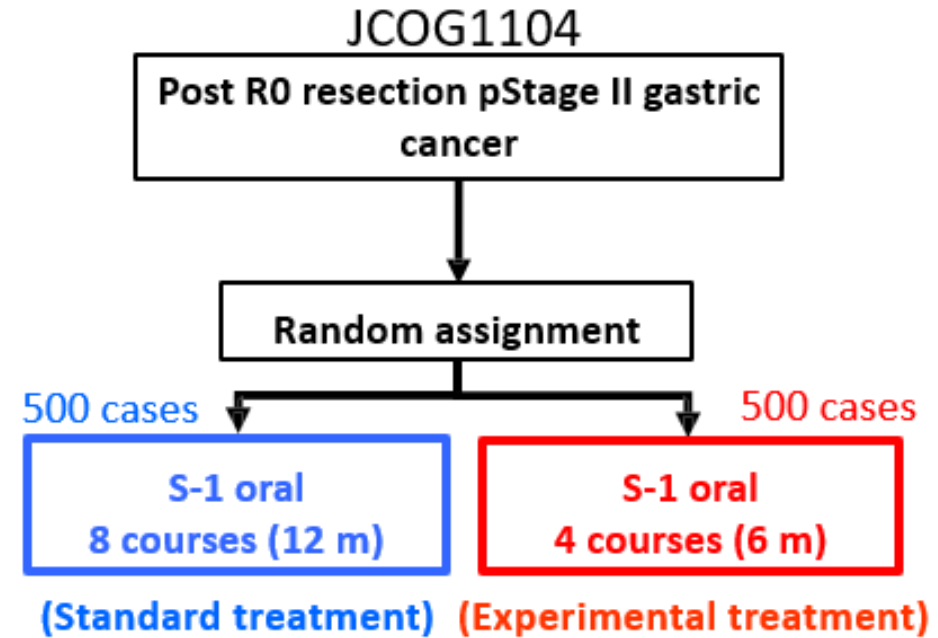
- Design: superiority or noninferiority
- Significance level: one-sided or two-sided, always 5%?
- Power
- Significance of treatment effect (clinical significance or expectation)

Superiority and Non-inferiority Tests



Superiority test

- Experimental treatment must be superior in efficacy
- Experimental treatment is inferior to standard treatment in terms of safety and other factors
(Toxic new)

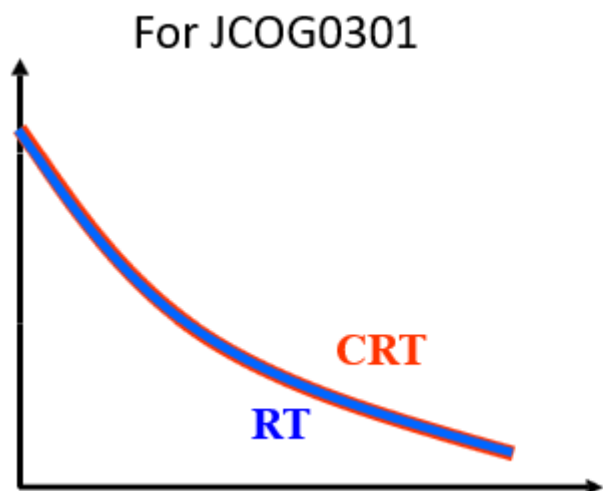


Non-inferiority test

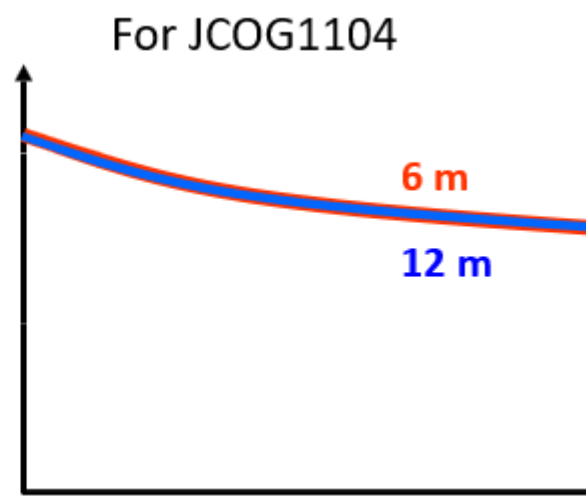
- Experimental treatment must be no less effective than the standard treatment
- Experimental treatment is superior to standard treatment in terms of safety and other factors
(Less toxic new)

Superiority/Non-inferiority Determination

- Decide on the situation in which **efficacy endpoints** (survival curves) overlap.
 - Select **standard treatment** → **Superiority trials**
 - Select **experimental treatment** → **Non-inferiority trials**



If the OS of the **CRT group** (**Toxic new**) and **RT group** are equivalent, the standard treatment is the **RT group**
→ **Superiority test**



If the RFS of the **6 m group** (**Less toxic new**) and the **12 m group** are equivalent, the standard treatment is the **6 m group**
→ **Non-inferiority test**

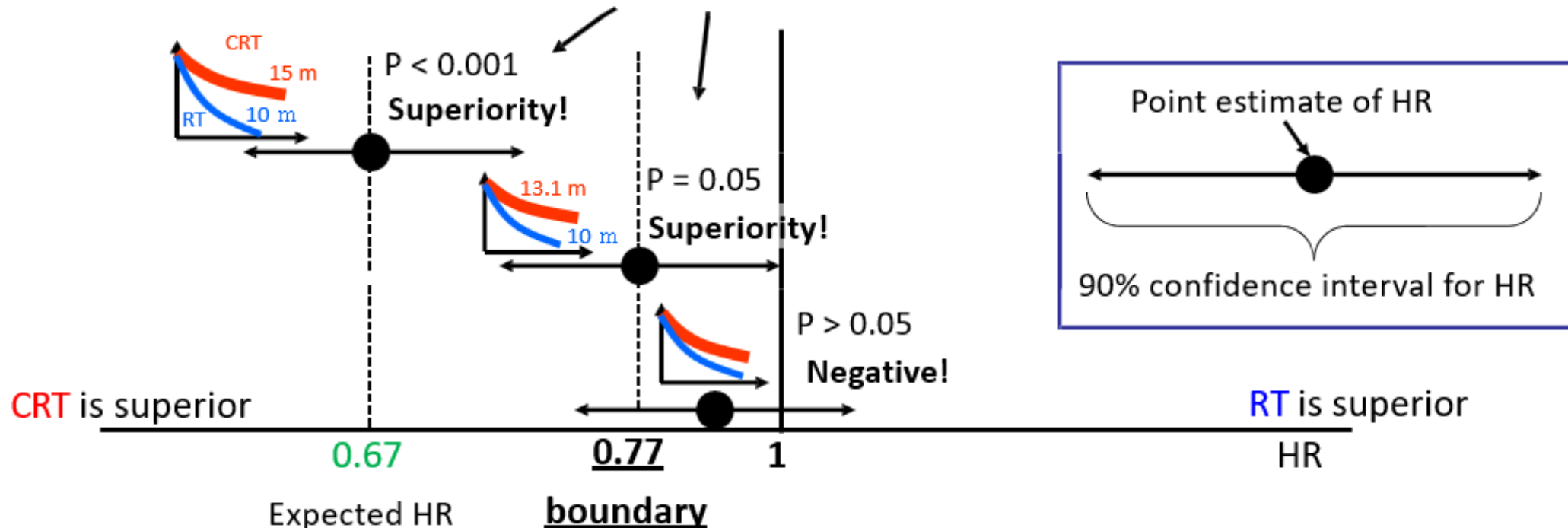
Statistical Significance and Boundary: The Case of Superiority Tests

- One-sided P value < 0.05 = 90% CI of two-sided hazard ratio (HR) is less than or equal to the null hypothesis (**HR = 1**)

Sample size design of JCOG0301

- One-sided $\alpha = 5\%$
- Power = 80
- MST for RT vs. CRT: 10 m vs. 15 m (HR = 0.67)
- Required number of participants for analysis (expected number of events): 174 cases (151) in total

Rather than HR = 1, CRT was shown to be superior

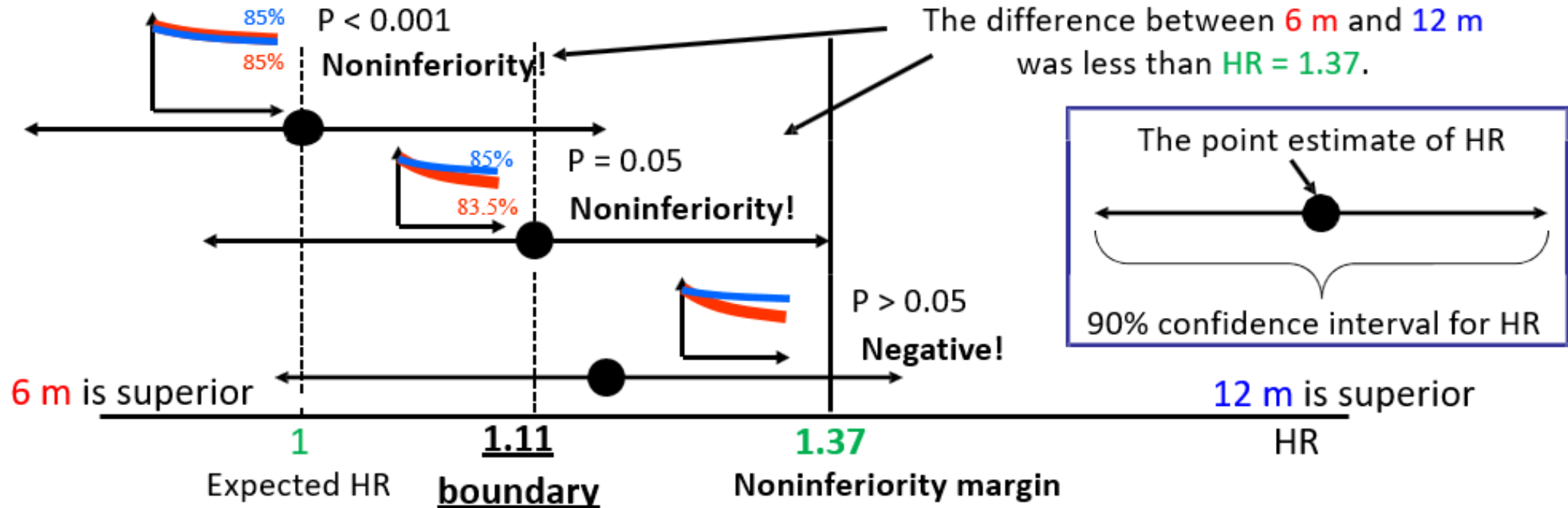


Statistical Significance and Boundary: The Case of Non-inferiority Trials

- Non-inferiority one-sided P value < 0.05 = two-sided 90% CI of HR is less than the null hypothesis (non-inferiority margin)

Sample size design of JCOG1104

- One-sided $\alpha = 5\%$
- Power = 80
- Three-year RFS (3yRFS) at 12 m vs. 6 m: 85% vs. 85% (HR = 1)
- Non-inferiority margin for HR: 1.37 (equivalent to 5% for 3yRFS)
- Required number of participants for analysis (expected number of events): 964 cases (246) in total

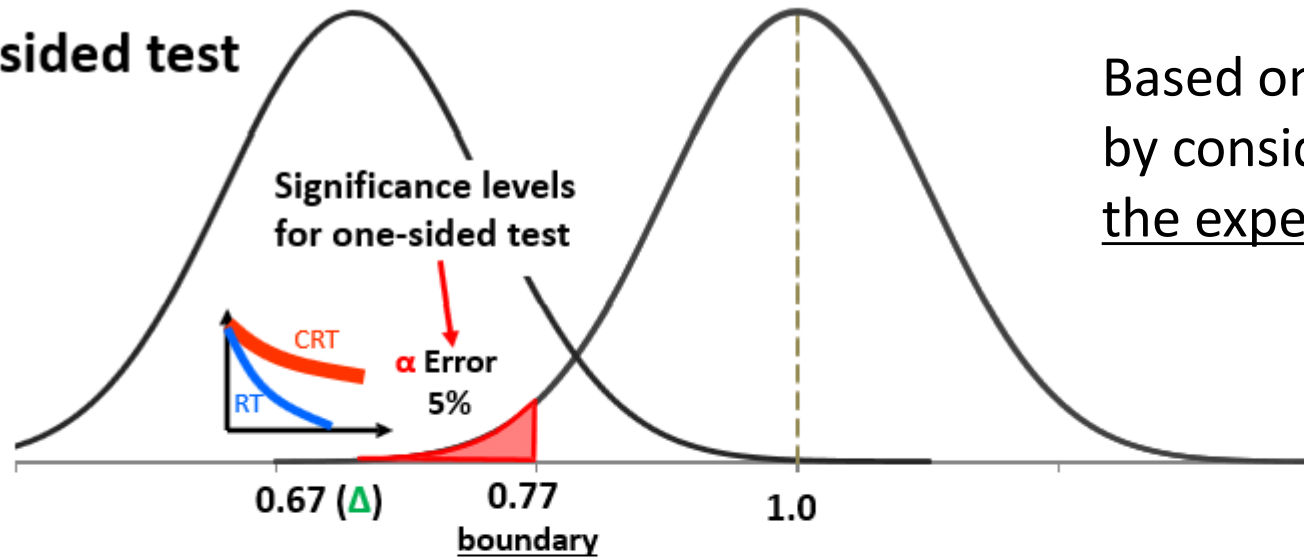


Things to Consider When Setting Parameters

- Design: superiority or noninferiority
- Significance level: one-sided or two-sided, always 5%?
- Power
- Significance of treatment effect (clinical significance or expectation)

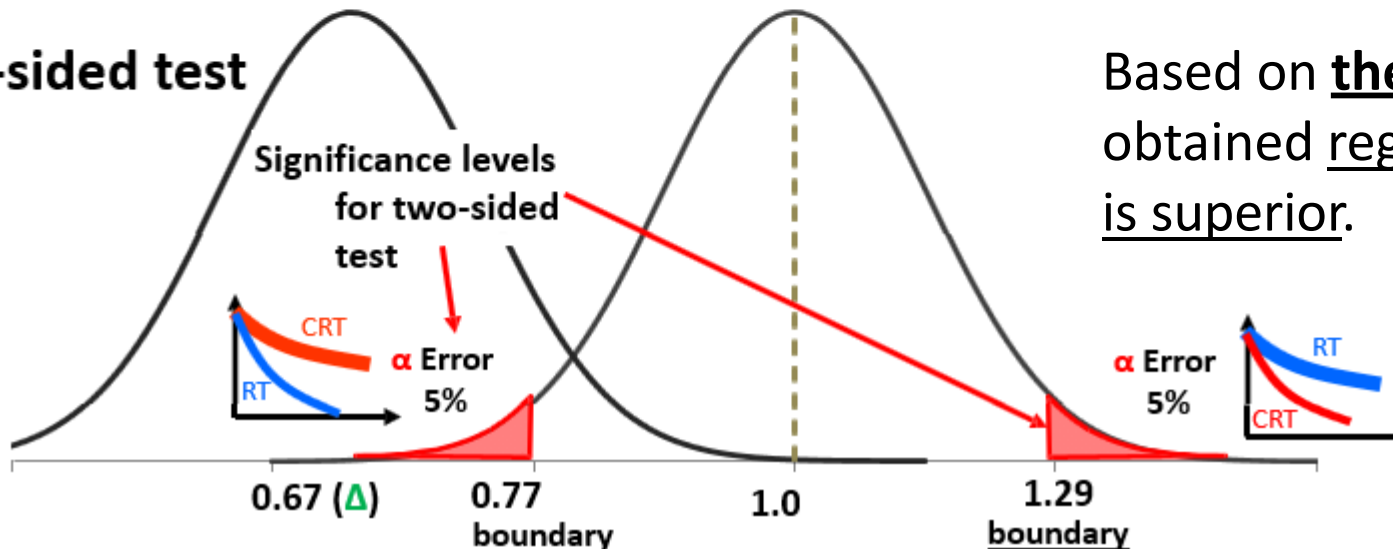
Significance Level α : One-sided and Two-sided Tests

One-sided test



Based on the one-sided P value obtained by considering only the direction in which the experimental treatment is superior.

Two-sided test



Based on the two-sided P values obtained regardless of which treatment is superior.

Two ways to decide whether to use a one-sided or two-sided test

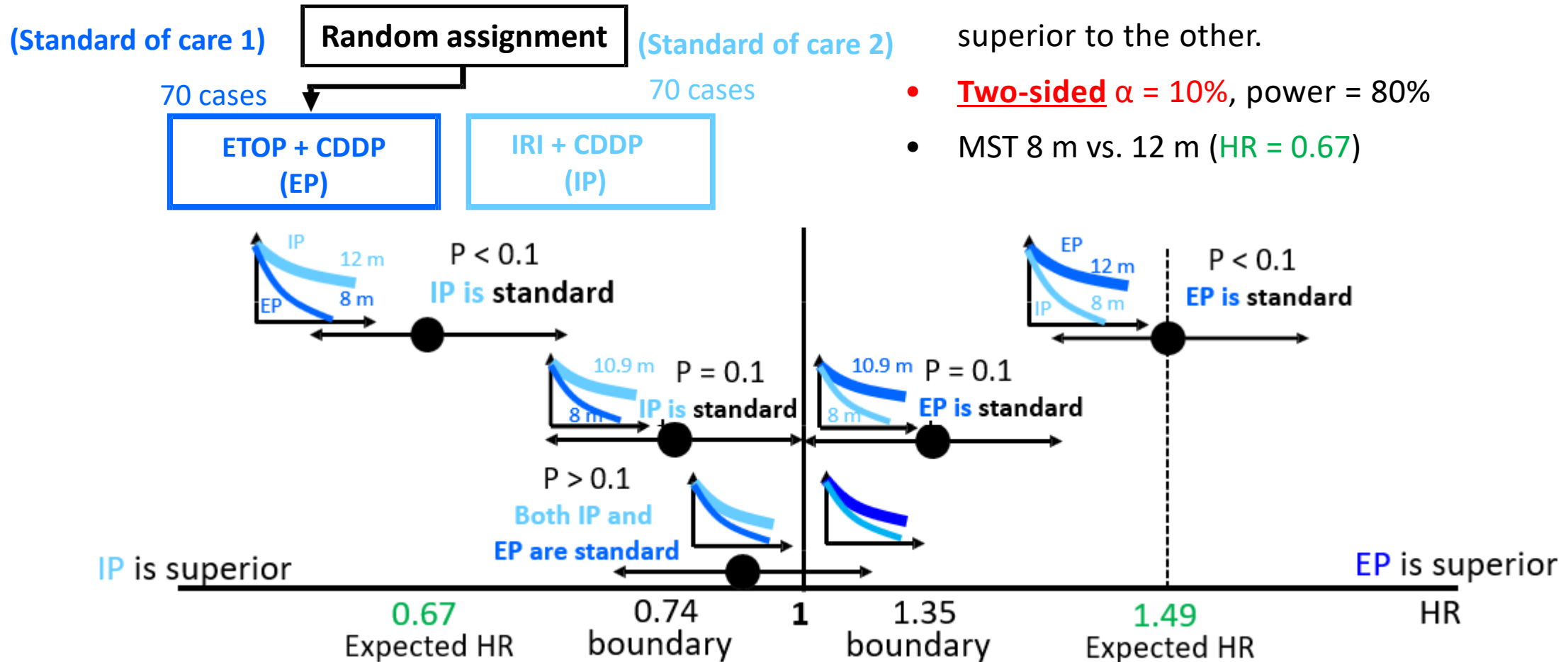
Recommended!

- A) Decide according to the decision-making process, considering the risks/benefits of the treatment
- JCOG0301 (superiority): in case of a comparison of RT vs. CRT: one-sided test
 - CRT that is Toxic new must be superior to RT
 - Not interested in CRT being significantly inferior to RT; even if CRT is not significantly inferior to RT in the interim analysis, the study will be terminated.
 - JCOG1104 (non-inferiority): In the case of a comparison of 12 m vs. 6 m: one-sided test
 - The less toxic 6 m is acceptable unless it is inferior to 12 m (it can be superior)
 - In cases where superiority is not allowed, equivalence testing, rather than non-inferiority testing, is required (e.g., for generic antihypertensive drugs).
 - If the risk-benefit ratio of the treatments is comparable (superiority [a test to prove a difference]): two-sided test
 - Either treatment may be superior, and if there is no significant difference, either treatment is the standard treatment (JCOG1213)
- B) Should always be a two-sided test if there is a possibility that the experimental treatment is inferior to the standard treatment
- Two-sided test to also prove that the experimental treatment is inferior
 - Even if highly toxic experimental treatments are found to be inferior in interim analysis, the trial will not be discontinued until they are significantly inferior.

Example of JCOG Study With Two-Sided α

JCOG1213

Gastrointestinal tract, hepatobiliary, and pancreatic primary
unresectable or recurrent neuroendocrine cancer



- Efficacy and safety are hard to choose Comparison of two standard treatments
- We are also interested in determining which one is superior to the other.
- **Two-sided** $\alpha = 10\%$, power = 80%
- MST 8 m vs. 12 m (**HR = 0.67**)

α Is Not Always 5%: Set α According to the Situation

- Two-sided $\alpha = 0.05$ or one-sided $\alpha = 0.025$
 - Global standard (**Phase III standard [ICH E9]**): There is no reason to comply
 - Changing from two-sided to one-sided does not reduce the sample size
 - Two-sided 5% corresponds to one-sided 2.5% (same sample size)
 - α error is a risk for the patient, so they should be kept as small as possible
- One-sided $\alpha = 0.05$ – 0.2
 - **Phase II**: Even if it mistakenly shows significance, it can be validated next in Phase III
- Two-sided $\alpha = 0.1$ – 0.2
 - Evaluation of bias when comparing **background factors** between groups
 - $P > 0.05$ can affect endpoint → it is wrong to uniformly say "N.S."
 - Test for differences in treatment effects between subgroups (**interaction effects**)
- Two-sided or one-sided $\alpha = 0.0001$ – 0.005
 - **Phase III**: Significance levels in **interim analysis** considering the multiplicity
 - Unless there is a significant difference, the trial will not be discontinued for efficacy during its course

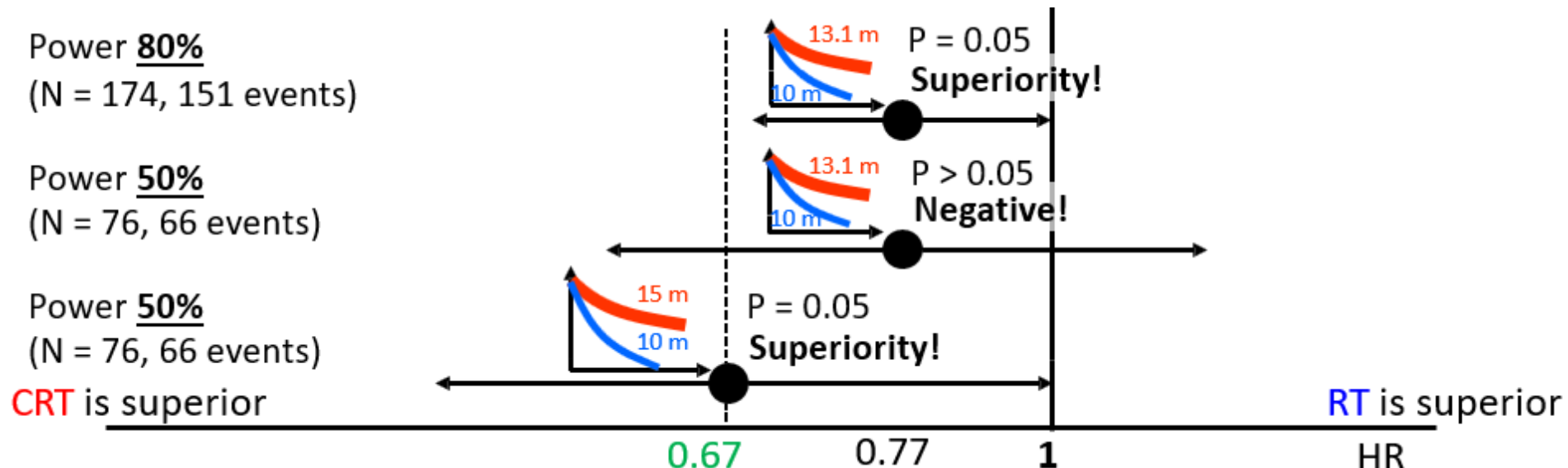
Things to Consider When Setting Parameters

- Design: superiority or noninferiority
- Significance level: one-sided or two-sided, always 5%?
- **Power**
- Significance of treatment effect (clinical significance or expectation)

Power Setting: 80% or more is the default

- Because **beta errors** are a risk for the researchers, they do not need to be as small as **α errors**.
 - Even if it is not significant, it will not be worse than the current situation.
- **Power 50%** = expected Δ is the boundary test
 - It is unethical because it is like flipping a coin to decide
 - There is no consensus on how much the statistical power can be reduced.

JCOG0301 example (one-sided $\alpha = 5\%$, MST 10 m vs. 15 m [HR = 0.67])



Things to consider when setting Parameters

- Design: superiority or noninferiority
- Significance level: one-sided or two-sided, always 5%?
- Power
- Significance of treatment effect (clinical significance or expectation)

Direction for Determining Δ

Common to superiority and noninferiority studies

- A) Decide on the risk-benefit of the treatment to be compared
 - Set the clinically meaningful difference to Δ
 - If the difference in toxicity is large, the Δ is large. If the difference is small, the Δ is small
 - Clinically meaningful differences are determined by consensus among researchers
 - To what extent of difference would be acceptable for adopting the new treatment?
- B) Decide based on the expected additional effect
 - If the likelihood of success is high, set a large Δ

In the case of a noninferiority test (how to determine the noninferiority margin)

- C) Decide to ensure that the product is superior to the placebo to a certain degree

Hypothetical Example of the planning Phase of JCOG0301 (Superiority Study)

RT group

- Assuming MST = **10 m**
- RT is 2 Gy/day, 5 days/week, 60 Gy
- AnyGrade3-4 $\leq 10\%$
- Grade 4 AE is 0%

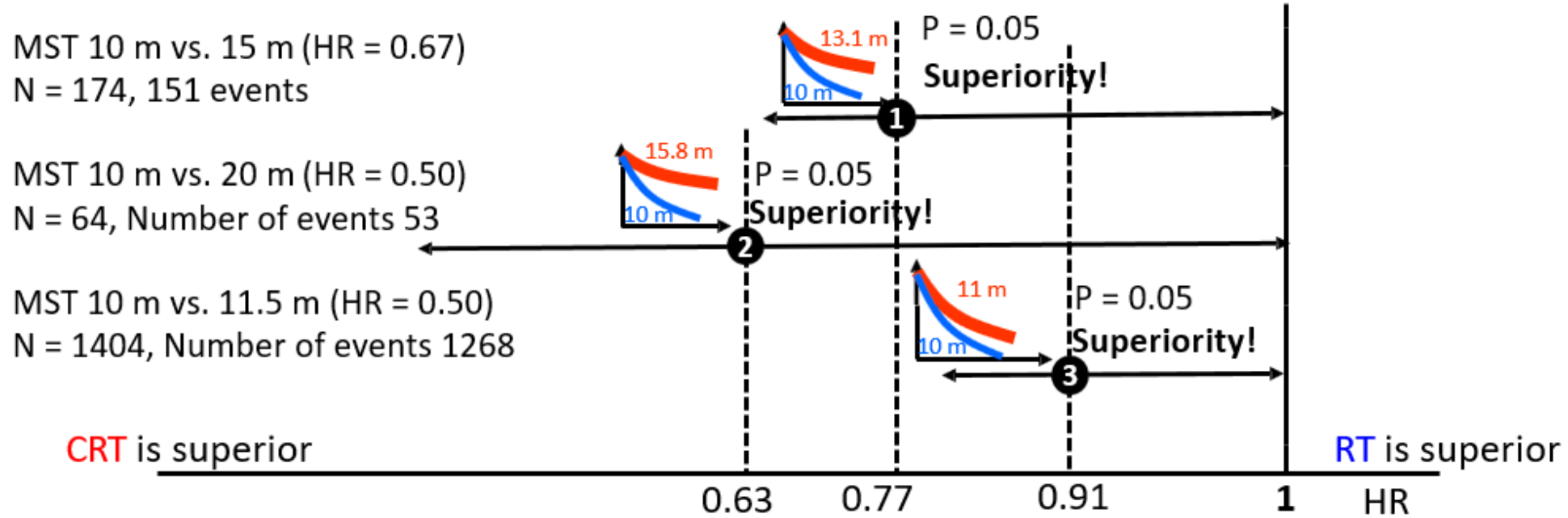
CRT group [low-dose daily CBDCA + RT]

- Phase II results, MST = **20 m**
- RT is 2 Gy/day, 5 days/week, 60 Gy
- Intravenous infusion of CBDCA is 30 mg/m² once daily within 1 h before the start of RT
- G4 neutropenia = 25%,
FN of G3 = 12.5%

- If there is an additional 5 m, it justifies the toxicity and effort involved
(= the least clinically meaningful difference)

Setting of Δ and Statistical Significance

Example of JCOG0301 (one-sided $\alpha = 5\%$, 80% power)



Recommended!

- (1) Detect clinically meaningful differences
- (2) The number of required analyses is reduced, but even if a clinically meaningful difference is obtained, it can no longer be considered statistically significant
- (3) Even clinically meaningless differences are judged to be statistically significant

Background of the JCOG1104 Study Plan

ACTS-GC
Post-gastrectomy stage II-III B gastric cancer
20–80 years old

Random assignment

529 cases

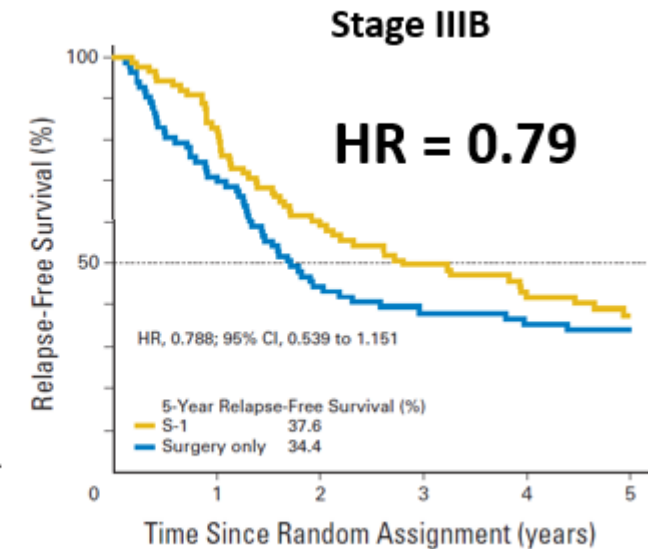
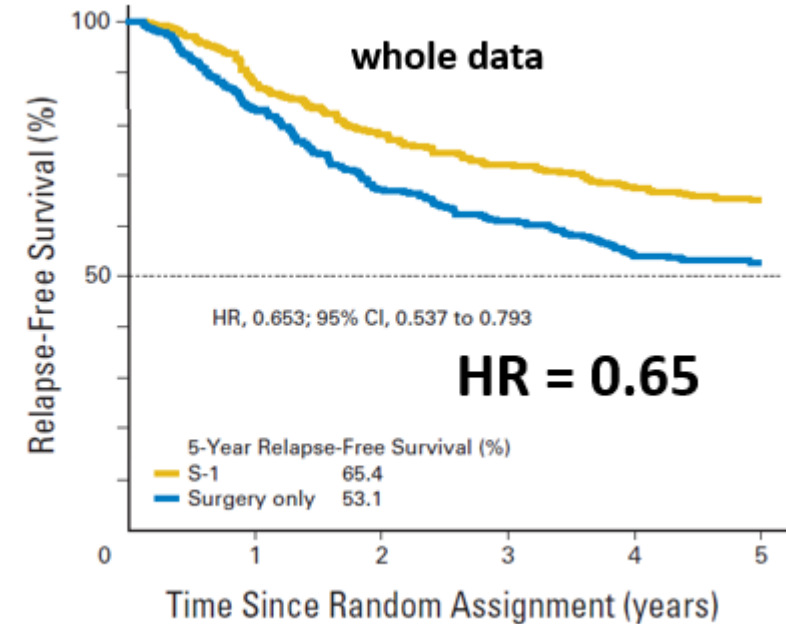
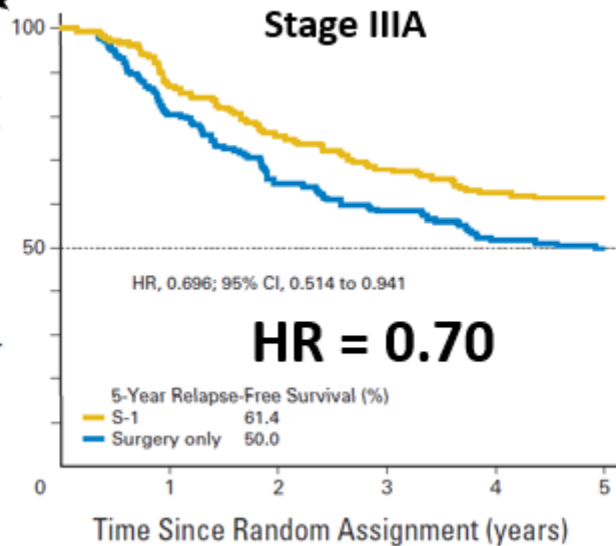
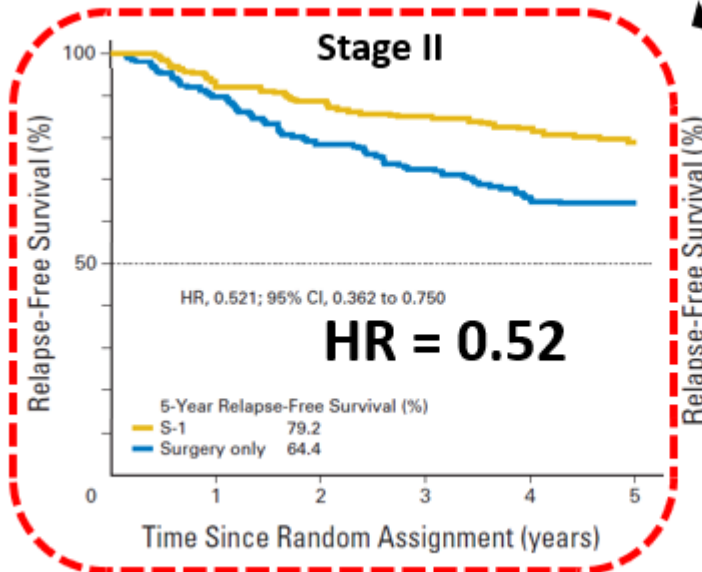
Follow-up
(surgery only)

(Standard treatment)

530 cases

S-1 1-year oral
(S-1)

(New treatment)



Sasako M. et al. J Clin Oncol. 29(33): 4387-93, 2011

Hypothetical Example of the Planning Phase of JCOG1104 (Non-inferiority Study)

S-1 12 m dose group

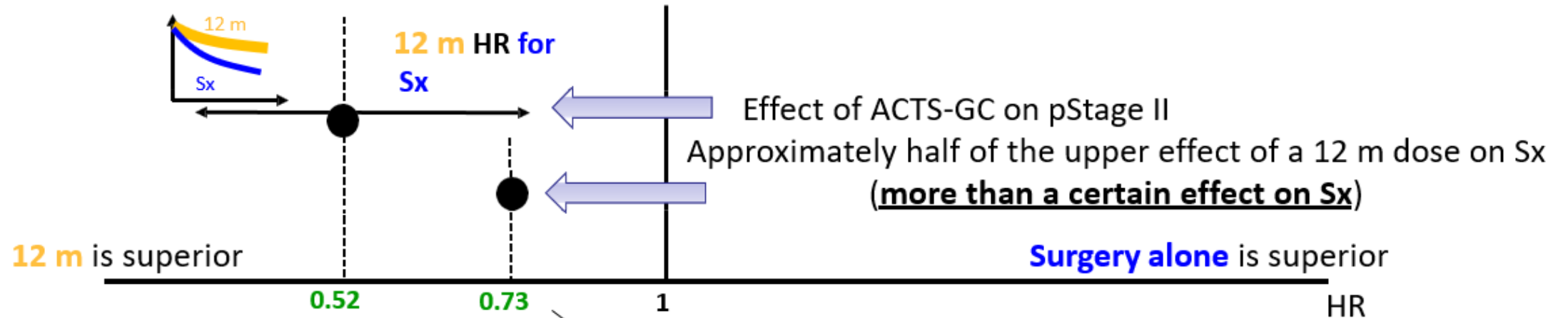
- Assumed 3yRFS = 85%
- Gastrointestinal toxicity for 1 year
 - Grade 2 or higher anorexia, nausea, diarrhea, fatigue, dermatitis ≥ 20
- Cost per year

- If the difference in 3yRFS is $\leq 5\%$ (non-inferiority margin of HR = 1.37), there is an advantage to administer for 6 m
- Is more than a certain level of effectiveness guaranteed for “Surgery alone”?

S-1 6 m dose group

- Assumed 3yRFS = 85%
- AEs that occur after 6 m disappear
 - Reduces the burden on patients, such as hospital visits
- Half the cost

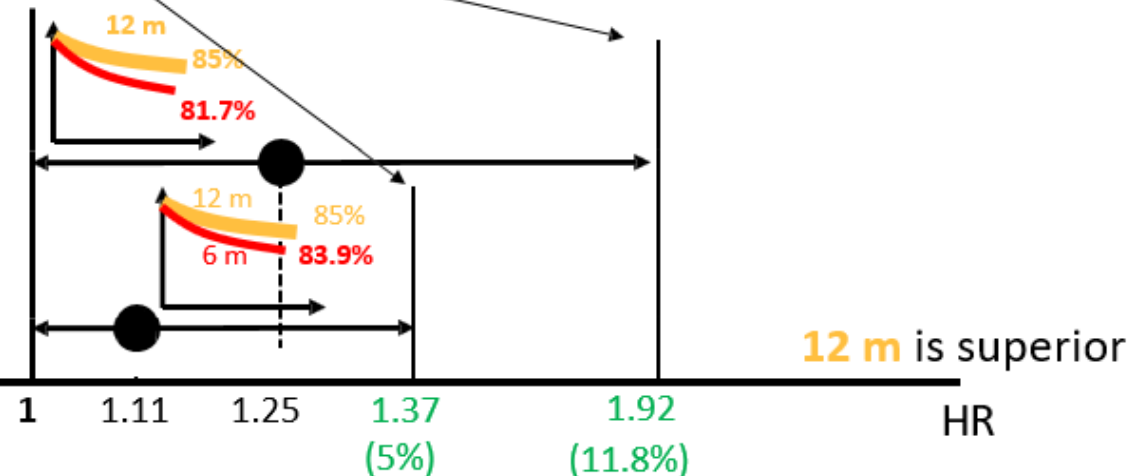
What Is More Than a Certain Level of Effectiveness for Surgery Alone?



The difference between 6 m and 12 m is HR = 1.92 or less
(only shown to be superior to Sx)

The difference between 6 m and 12 m is HR = 1.37 or less
(Guaranteed to be more than a certain level
of effectiveness for Sx of 12 m)

6 m is superior



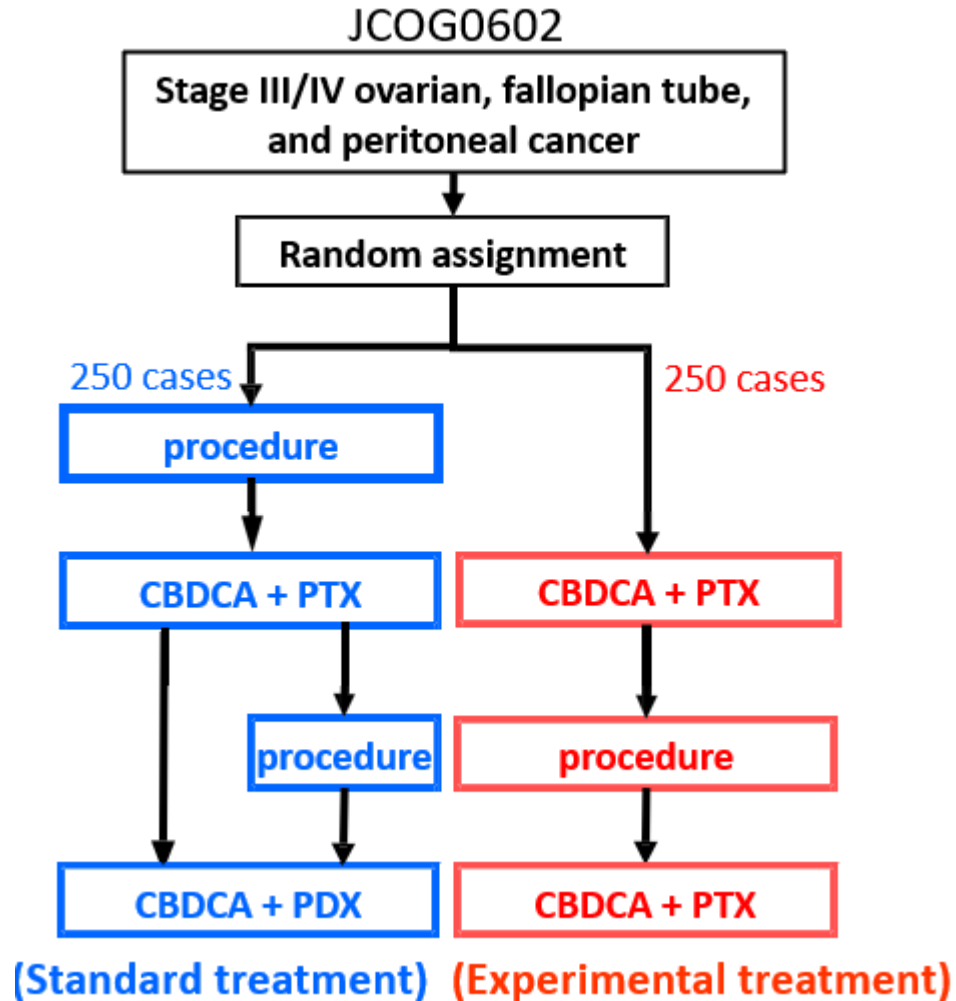
Non-inferiority Trial Design with a Reasonable Chance of Success



- Sample sizes for non-inferiority tests with a small inferiority margin and superiority tests with small differences are almost identical.
- Well-designed non-inferiority tests can be extensive.
- If the new treatment is expected to be less toxic and more effective, is it possible to design a feasible sample size?

Freidlin B, Korn EL, George SL, Gray R. J Clin Oncol. 2007; 25(31): 5019-23.

Examples of Non-inferiority Trial Designs with a Reasonable Chance of Success



Rationale for non-inferiority design

- If OS is the same, choose **experimental treatment**
 - Only one surgery is required
 - Reduction of surgery-related complications by post-NAC surgery

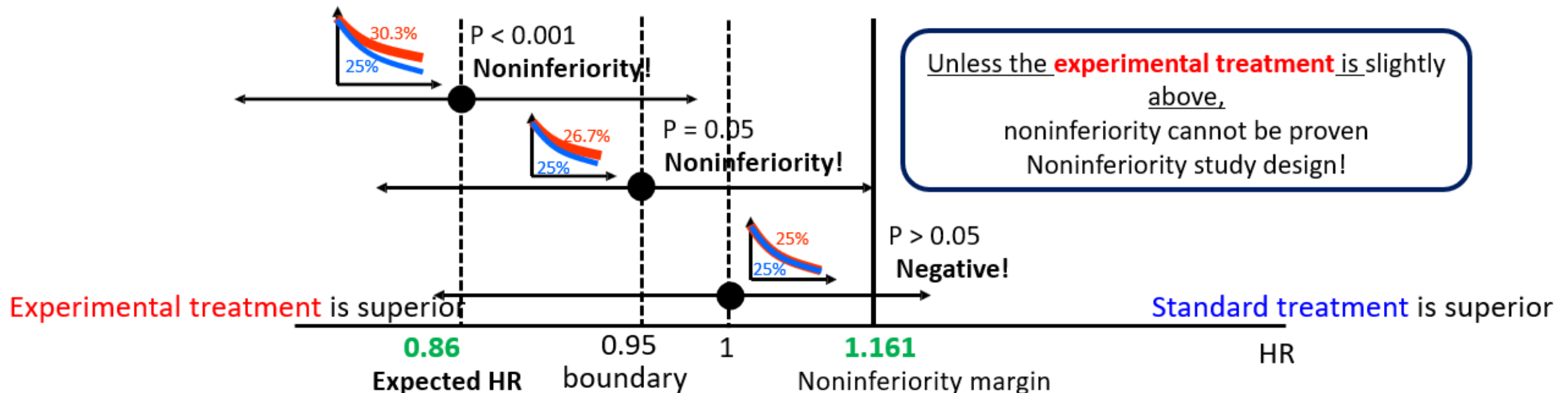
Rationale for a reasonable chance of success

- Early NAC
- Surgery of residual <1 cm tumor can be performed with improvement

Boundary of JCOG0602

Sample size design of JCOG0602

- One-sided $\alpha = 5\%$
- Power = 80
- 3yOS of **standard** vs. **experimental treatment**: 25% vs. 30.3% (HR = 0.86)
- Non-inferiority margin for HR: **1.161** (equivalent to 5% in 3yOS)
- Required number of participants for analysis (expected number of events): 298 cases in total (278)
- When HR = 1 for standard vs. experimental, the number of required analyses (events): 1174 (1110)



What Type of Test Design Would You Use?

For stage IIIB/IV, post-platinum therapy for non-squamous non-small cell lung cancer,
docetaxel vs. **nivolumab** (for simplicity, cost shall not be considered)

Some figures are hypothetical

Docetaxel

- Highly toxic
 - Any AE grade 3-4 50% or more
 - G3-4 Fatigue 10
 - G3-4 neutropenia 30%
 - FN 10%
 - Any AE grade 1-4 86%
- MST = approximately 8 m

Nivolumab

- Low toxicity
 - Any AE grade 3-4 7%
 - G3-4 Fatigue 1
 - G3-4 leukopenia 1%.
 - Others 0%
 - Any AE grade 1-4 58%
- MST = about 12 m

(1) Superiority test

(2) Non-inferiority test

(3) Non-inferiority test with a chance of winning

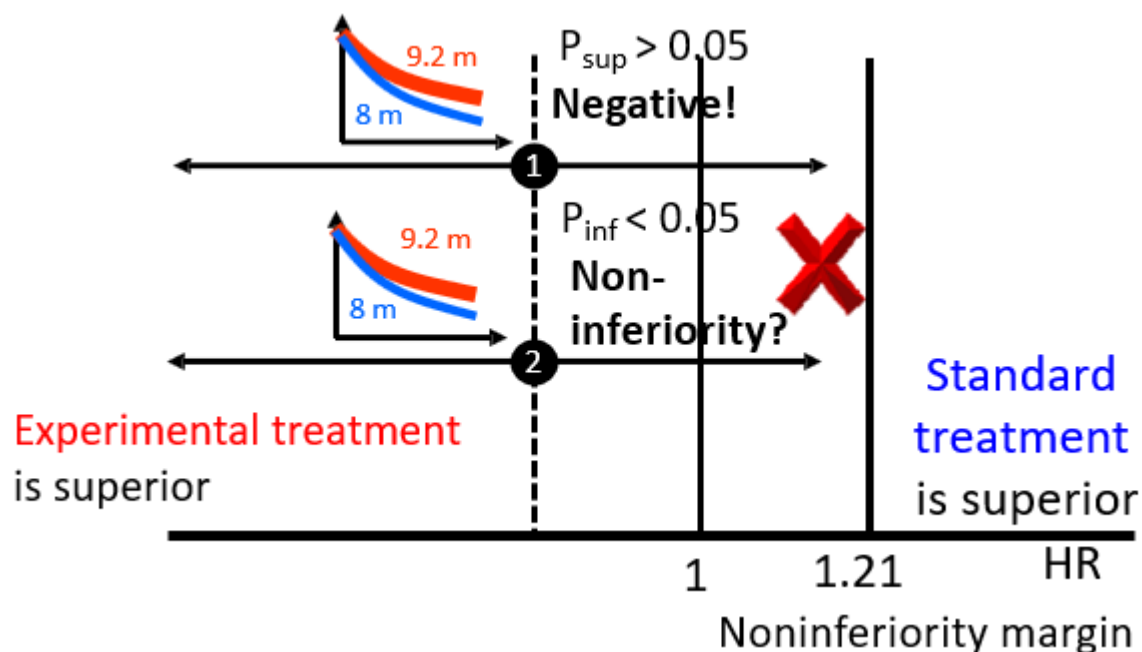
If superiority is achievable, it is hard to settle for non-inferiority...
In a non-inferiority trial, you cannot claim superiority, can you?



It Is Possible to Claim Superiority Even with a Non-inferiority Design Setup

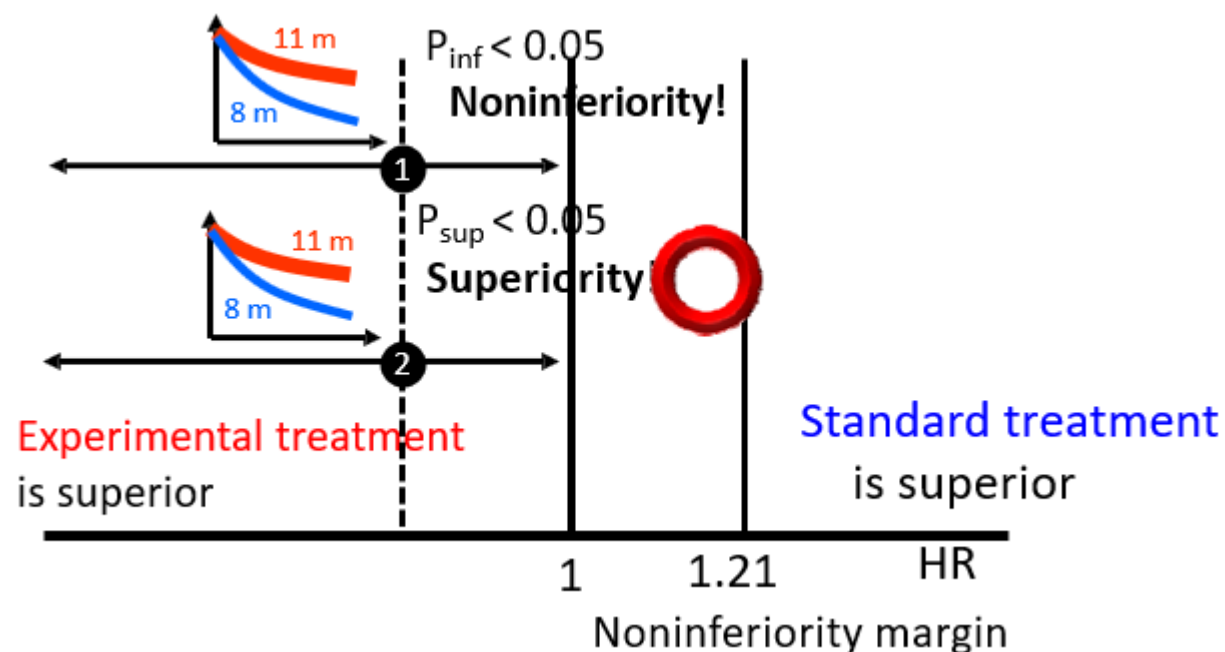
In the case of superiority design

When superiority is not displayed, the non-inferiority hypothesis cannot be retroactively analyzed.



In the case of non-inferiority design

It is acceptable to analyze the superiority hypothesis when non-inferiority has been demonstrated.



Sample Size Calculation

– In the Case of a Group Comparison of Survival

Required Information for Calculating Sample Size for Survival Analysis

- Significance level: α
- Power: $1-\beta$ (=power)
- Size of treatment effect: Δ
 - Δ is a relative value (HR) rather than an absolute value (5yOS or MST)
 - Assuming an exponential curve, convert 5yOS and MST delta to HR

- Estimation of prognosis for the target population
- Enrollment period
- Follow-up period

Support the **variability** of sample size calculation formula

The Power of a Survival Analysis is Determined by the Number of Events

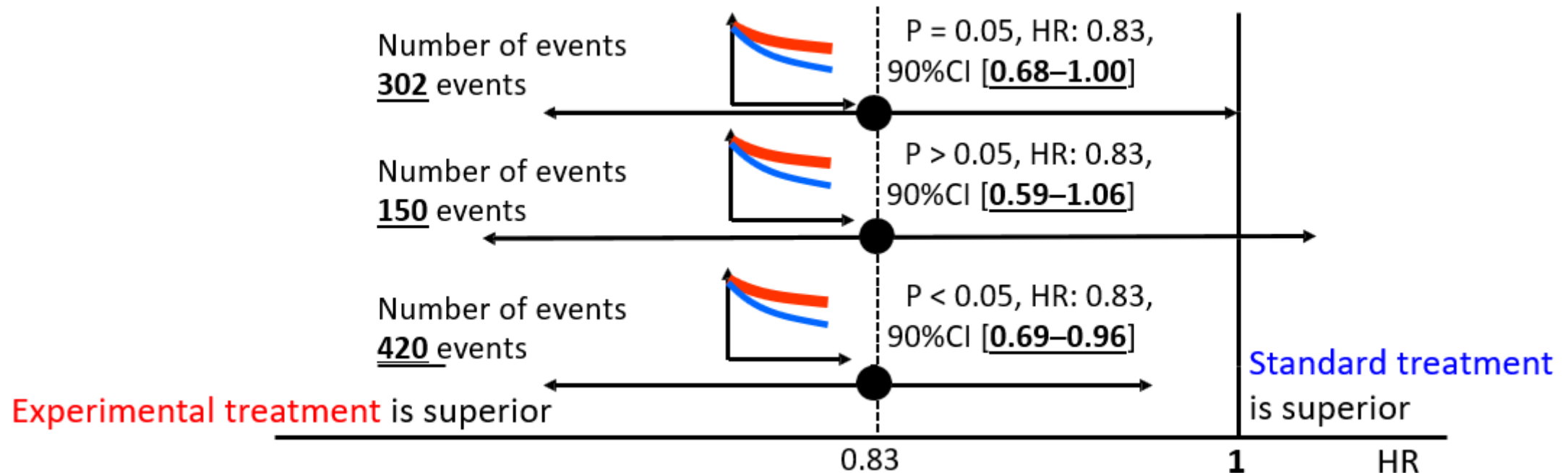
- 10000 cases enrolled and 100 events
- 1000 cases enrolled and 100 events
- 100 cases enrolled and 100 events

All have the same power

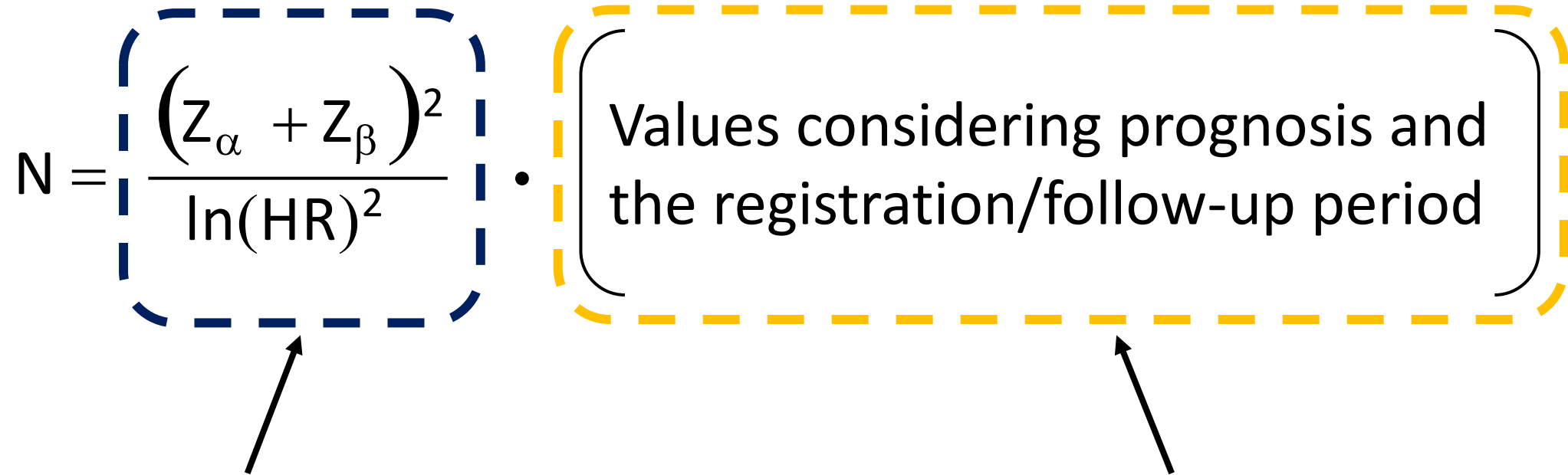
(If the point estimates of HR are the same, the confidence intervals are also the same)

“How many events occurred?” is more important than “How many cases have been enrolled?”

The number of events determines the width of the confidence interval



Sample Size Calculation Procedure for Survival Analysis

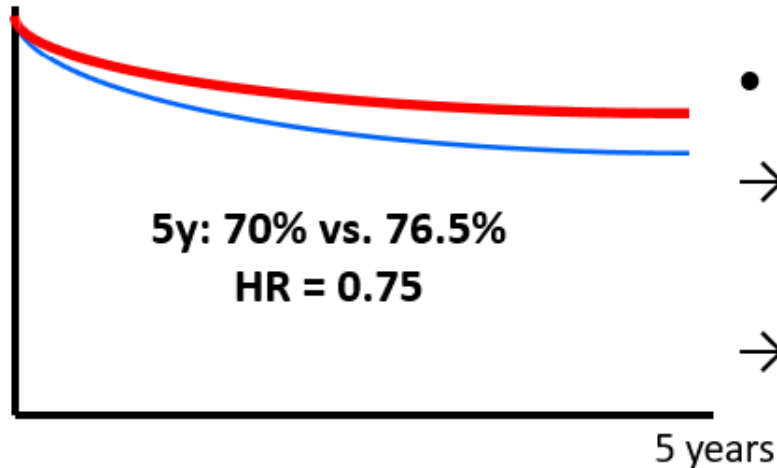
$$N = \left[\frac{(Z_{\alpha} + Z_{\beta})^2}{\ln(HR)^2} \right] \cdot \left[\text{Values considering prognosis and the registration/follow-up period} \right]$$
The diagram illustrates the sample size calculation formula for survival analysis. The formula is presented as $N = \left[\frac{(Z_{\alpha} + Z_{\beta})^2}{\ln(HR)^2} \right] \cdot \left[\text{Values considering prognosis and the registration/follow-up period} \right]$. The first part of the formula, $\left[\frac{(Z_{\alpha} + Z_{\beta})^2}{\ln(HR)^2} \right]$, is enclosed in a blue dashed box. An arrow points from this box to step (1) below. The second part, $\left[\text{Values considering prognosis and the registration/follow-up period} \right]$, is enclosed in a yellow dashed box. An arrow points from this box to step (2) below.

(1) Calculate the number of events required by α , β , and Δ

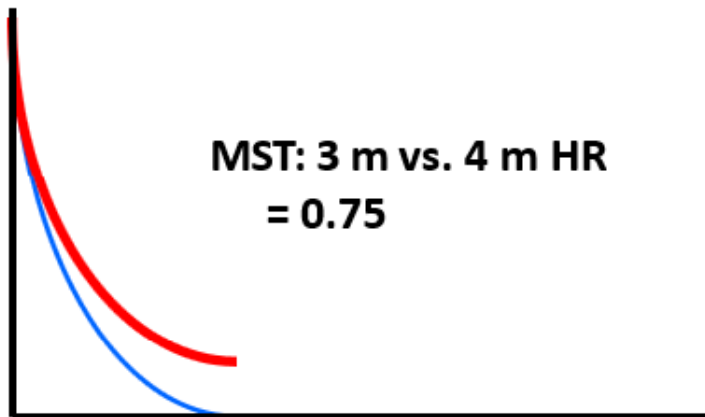
(2) Calculate the N necessary to obtain the required number of events

Number of participants required to observe 380 events

For one-sided $\alpha = 2.5\%$, power 80%, HR = 0.75, about 380 events required



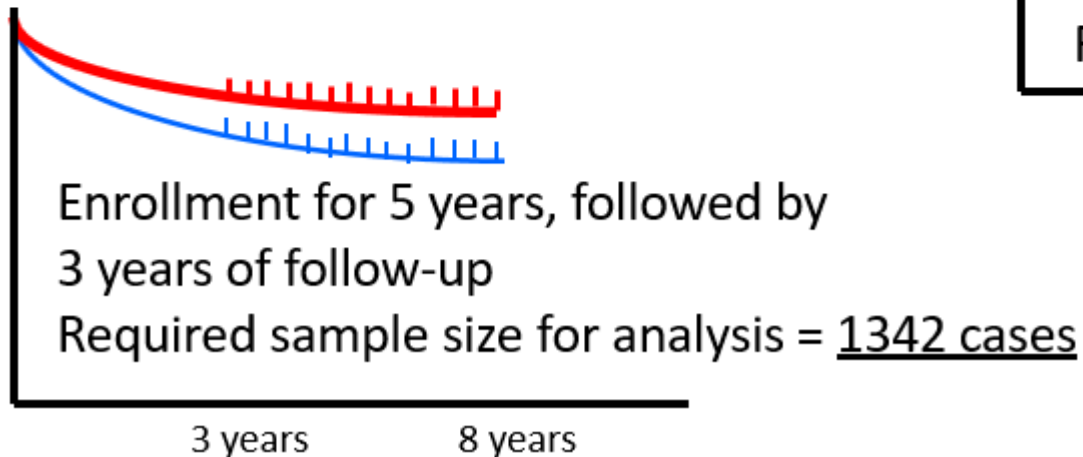
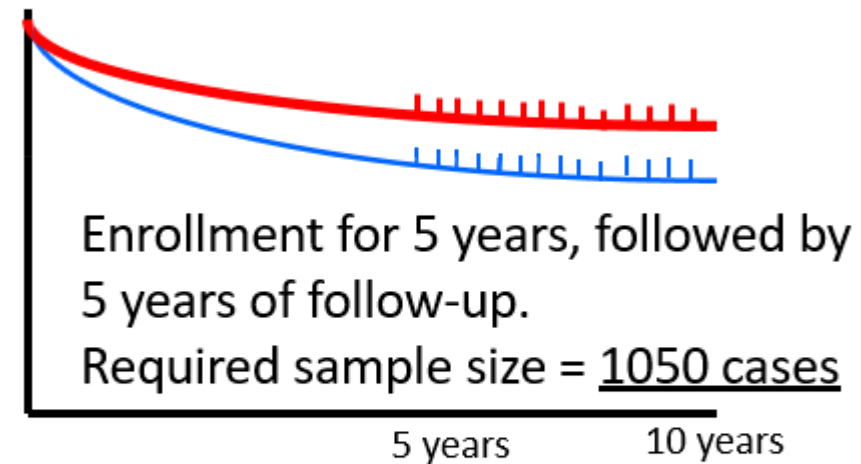
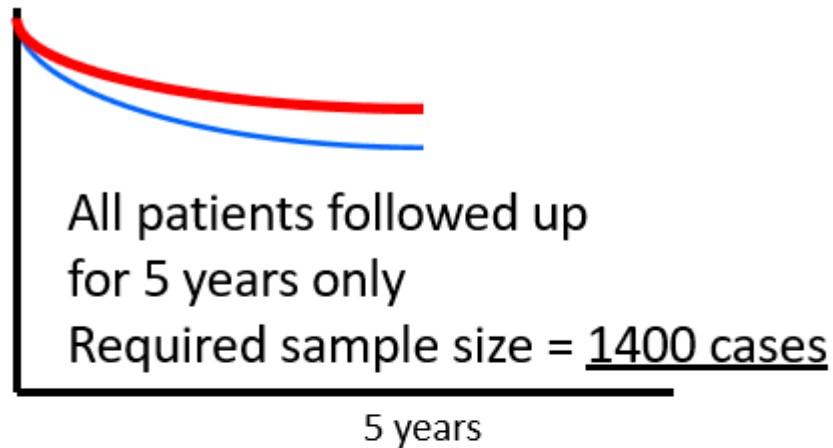
- Pooled groups 5y $\approx 73\%$
→ 27% of enrolled patients
If an event occurs, 380 events
→ Number of samples required = $380 \div 0.27 \approx 1400$ cases



- Almost all enrolled patients have an event
→ Number of required analyses \approx Number of required events
→ Number of cases required for analysis ≈ 380 cases

Consider Events That Occur during the Enrollment/Follow-up Period

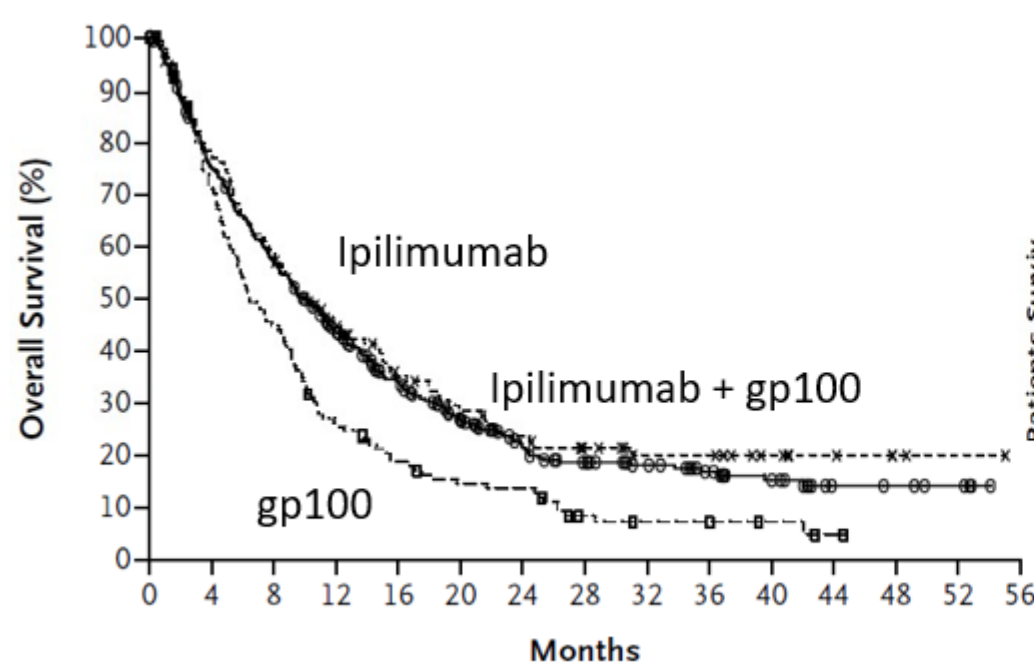
For one-sided $\alpha = 2.5\%$, power 80%, HR = 0.75, approximately 380 events are required 5 years: 70% vs 76.5% (HR = 0.75)



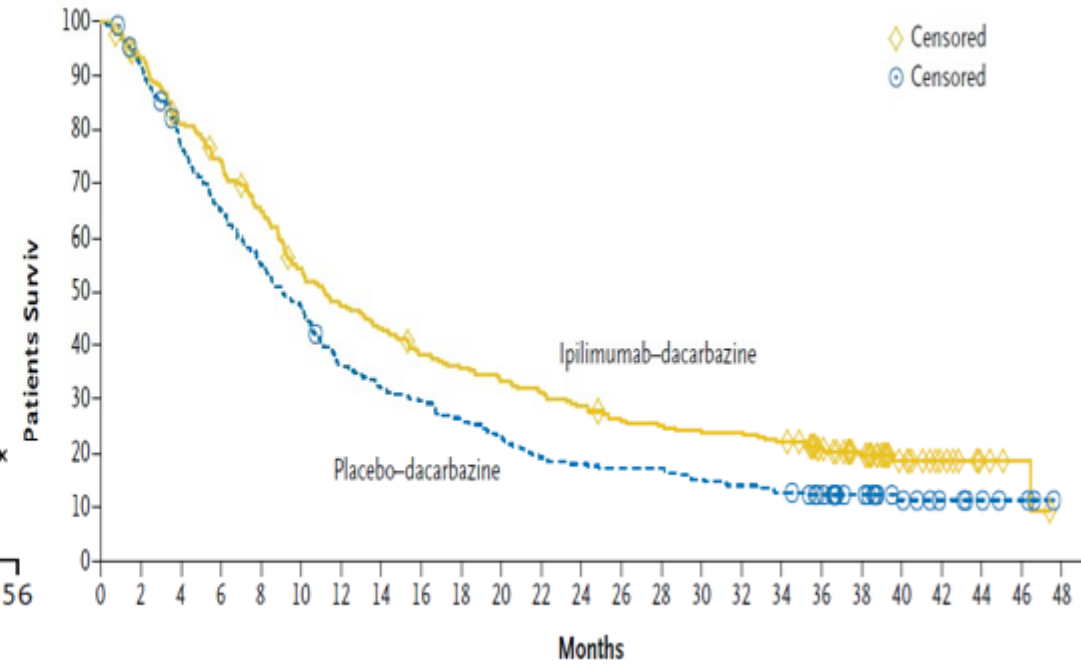
Assumptions of the Sample Size Calculation Method for Standard Survival Analysis

- Both groups assume an exponential curve
 - What if the exponential curve does not hold?
 - Participants with good prognosis plateau in the middle of the curve and are undetectable.
- The proportional hazard property is established
 - What if the proportional hazard property does not hold?
 - If the curves overlap up to a certain point and move apart after that point, that is insufficient power.

Application: Sample Size Calculation for Immunotherapy



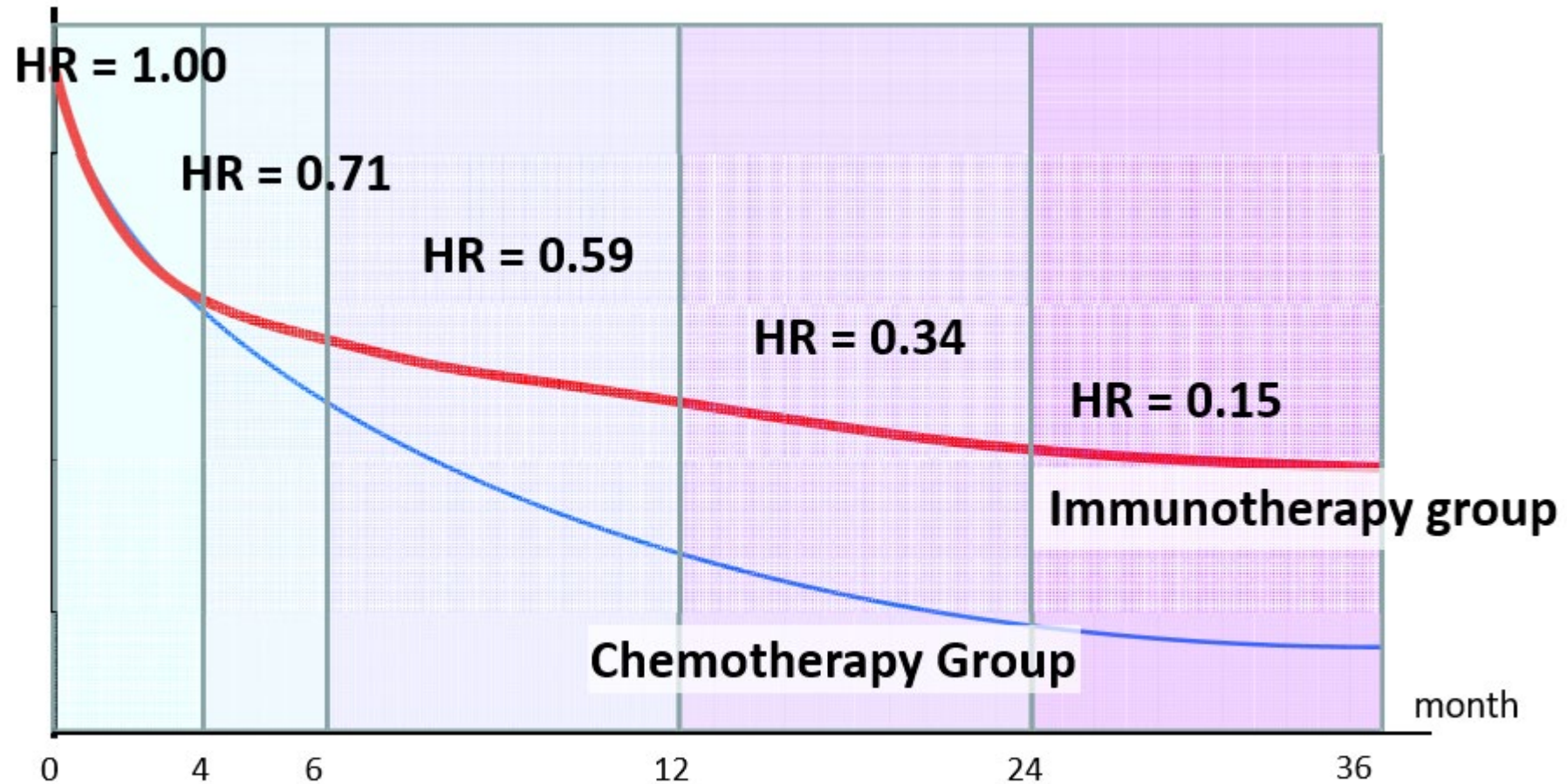
Hodi, F. Stephen, et al. N Engl J Med. 363.8 (2010): 711-723.



Robert, Caroline, et al. N Engl J Med. 364.26 (2011): 2517-2526.

- The proportional hazards assumption is violated
 - No effect for the first 4 months
 - A certain number of patients are cured
- Power is insufficient at a sample size calculation assuming an exponential curve for both groups

Assume Separate Exponential Curves for Each Section of the Curve



<http://www.nejm.org/doi/full/10.1056/NEJMoa1507643#t=abstract>

http://www.nejm.org/doi/suppl/10.1056/NEJMoa1507643/suppl_file/nejmoa1507643_protocol.pdf

Summary

- Parameters required for determining sample size are α , β , Δ , and variability
- Number of events, not N, is important in intergroup comparison of survival time
- Sample size calculation is a collaborative effort between statistician and clinician
 - In particular, the determination of Δ is a parameter for which the clinician is primarily responsible
 - Clarifying the clinical question is essential for determining Δ
 - Superiority or noninferiority
 - One-sided α or two-sided α
 - Clinically meaningful difference (Δ)
- There is no need to memorize detailed calculation methods
 - Calculations can be performed on software
 - Examine the validity of the design and parameters with a statistician